

# 重イオン衝突物理での ジェットの理解へむけて

*Nagoya University*  
Chiho Nonaka

July 10, 2009@第6回Heavy Ion Pub

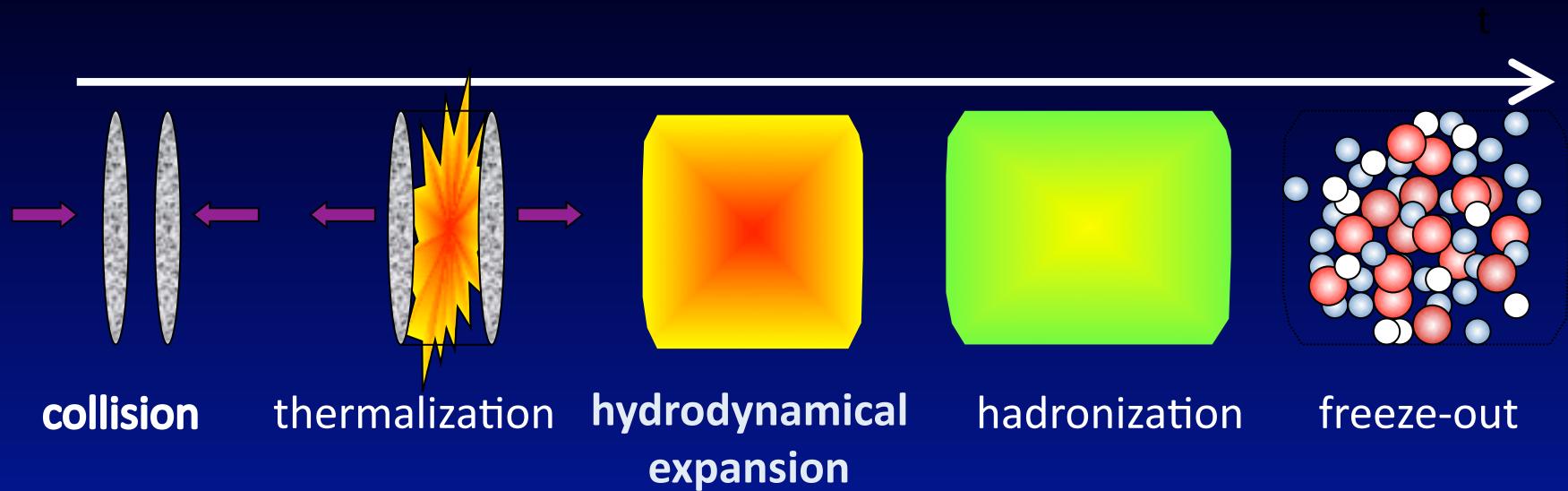
# Jet Quenching

- ❖ 1990
  - Jet Quenching in lepton nucleus scattering, Gyulassy and Plumer
  - Jets in heavy ion collisions, X-N. Wang and Gyulassy
- ❖ RHIC
  - QM2001
  - Key issue
  - X-N.Wang
    - Event generators –Quo Vadis?
    - HIJING

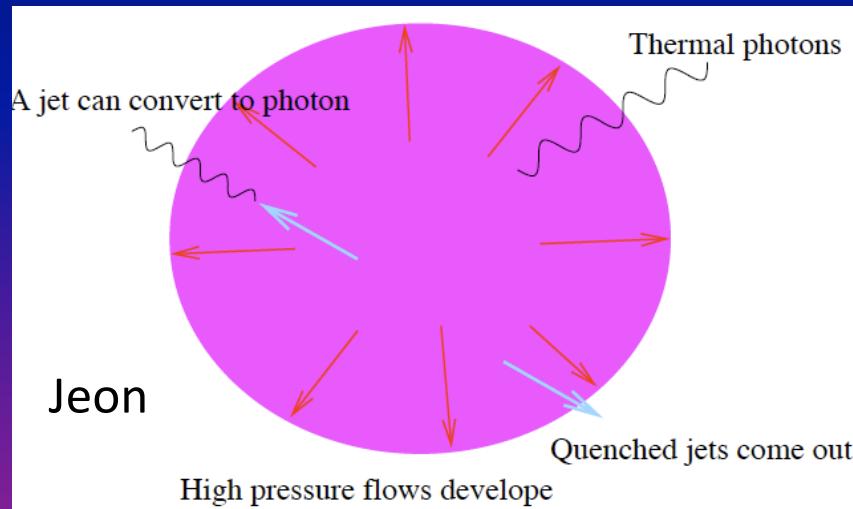
Heavy Ion Pub @Osaka University  
Perturbative QCD and Heavy Ion Collisions

# Relativistic Heavy Ion Collisions

## ❖ Schematic Sketch



Dynamics of  
Hot QCD matter



Jet quenching  
mechanism

# Phenomena

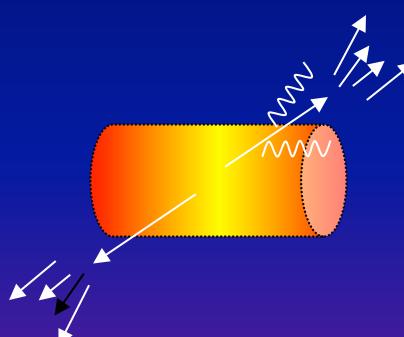
- ❖ Nuclear modification factors
- ❖ Jets structure
  - Azimuthal angle
  - 3 particle correlations
  - $\Delta \eta$  and  $\Delta \phi$

# Phenomena

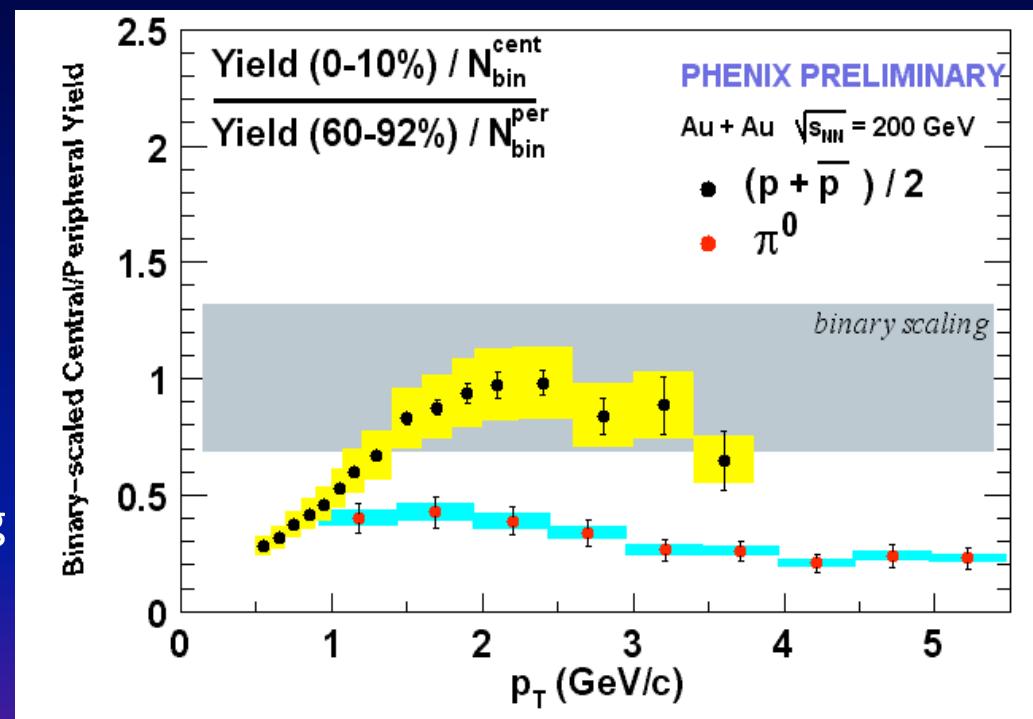
## ❖ Nuclear modification factors

## ❖ Jets structure

- Azimuthal angle
- 3 particle correlations
- $\Delta \eta$  and  $\Delta \phi$



- hard scattering in medium
- jet quenching

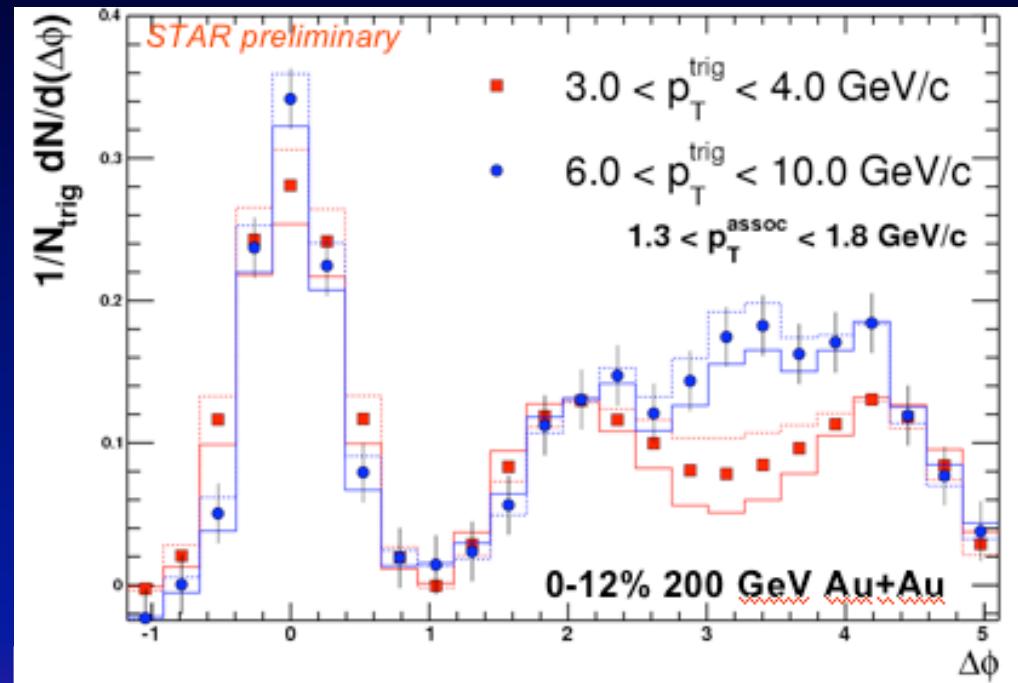
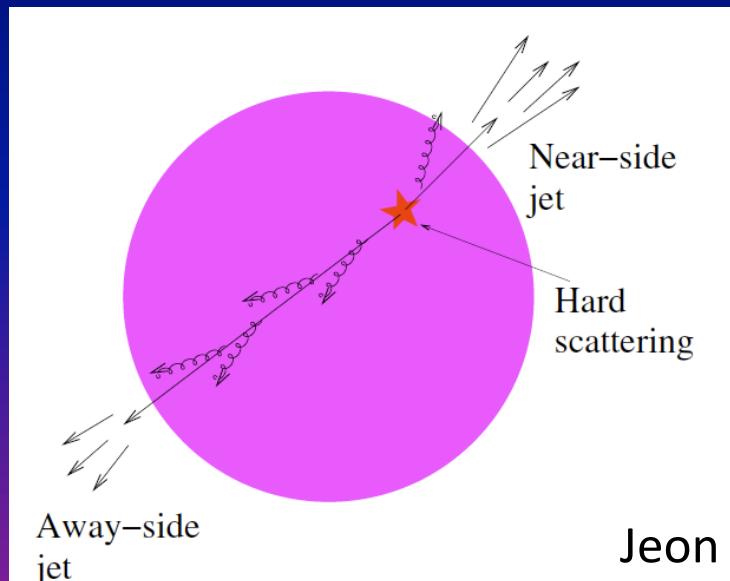


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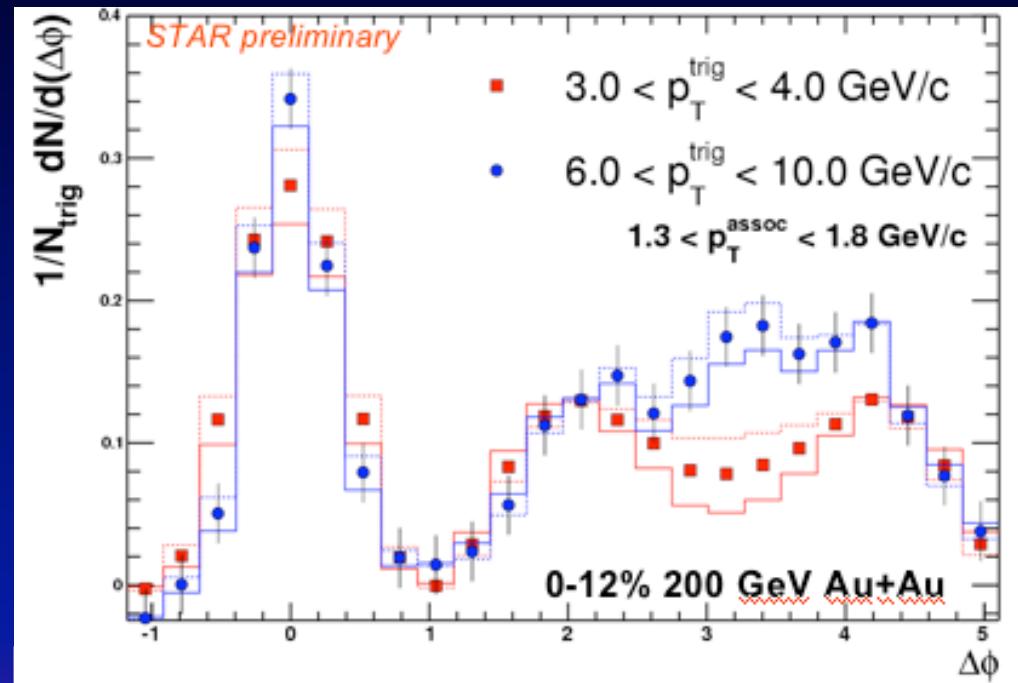
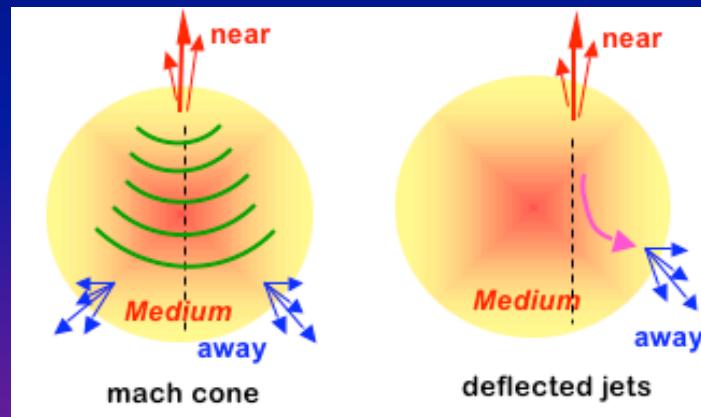


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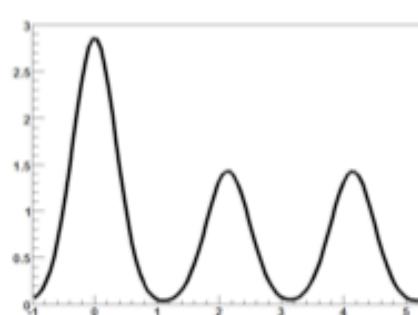
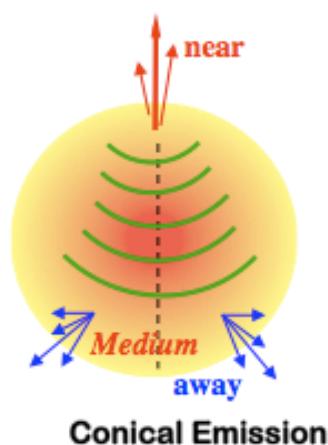
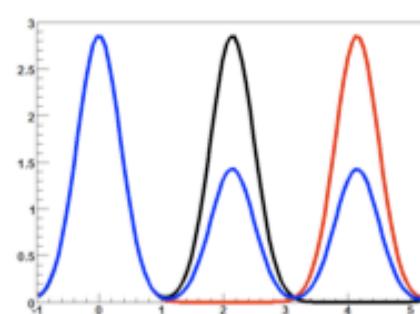
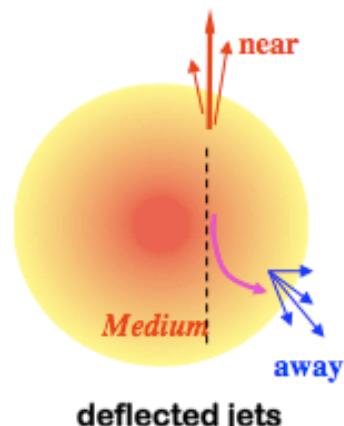
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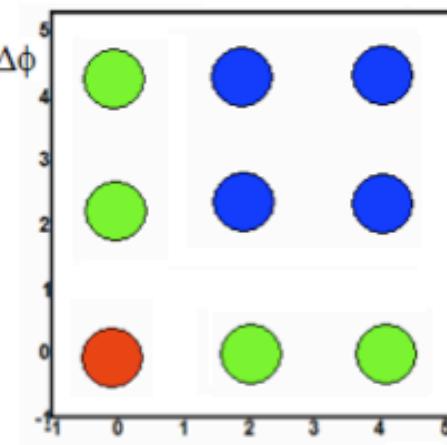
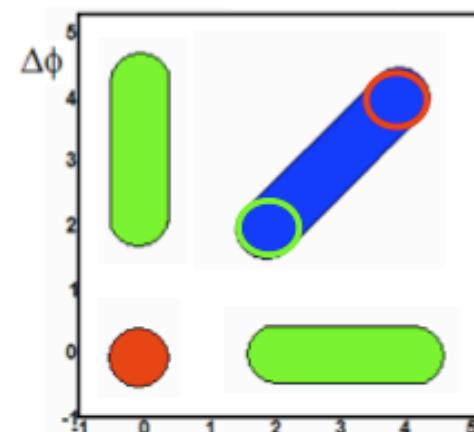
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- $\Delta\eta$  and  $\Delta\phi$



## Azimuthal 3-Particle Correlations



From : Jason Glyndwr Ulery  
(QM 2008)

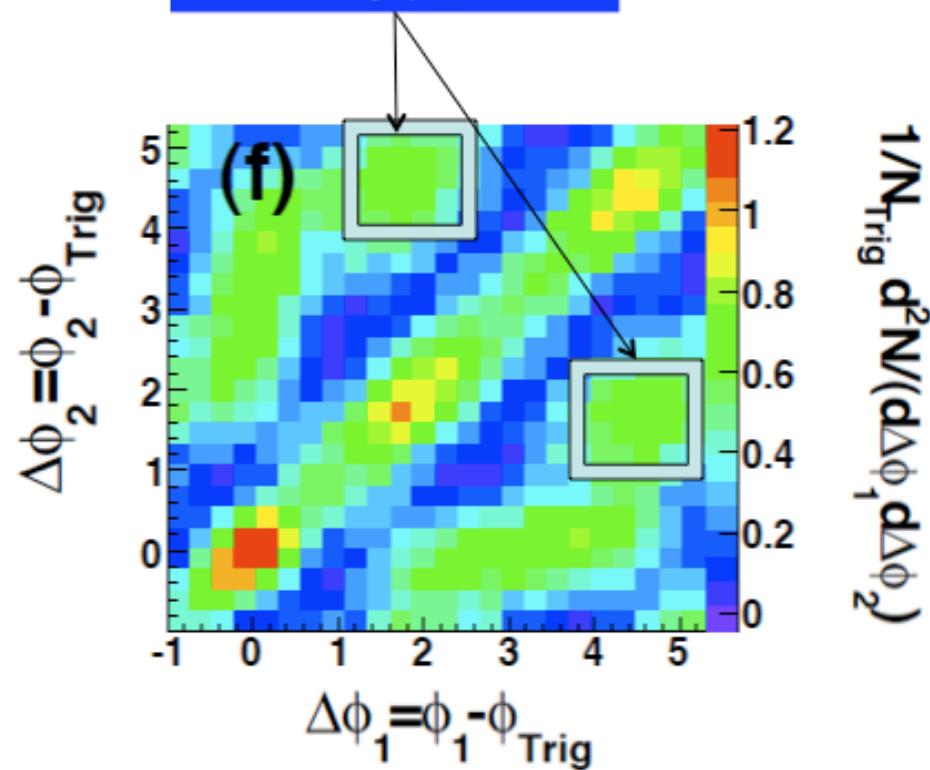


Chujo@Nagoya  $\Delta\phi$

## (f) Au+Au 0-12%

Off-diagonal成分  
の出現

B.I. Abel et al. (STAR),  
arXiv:0805.0622v1



Trigger particle ( $3 < p_T < 4$  GeV/c),  
Associated particle ( $1 < p_T < 2$  GeV/c).

Chujo@Nagoya

# Phenomena

- ❖ Nuclear modification factors

- ❖ **Jets structure**

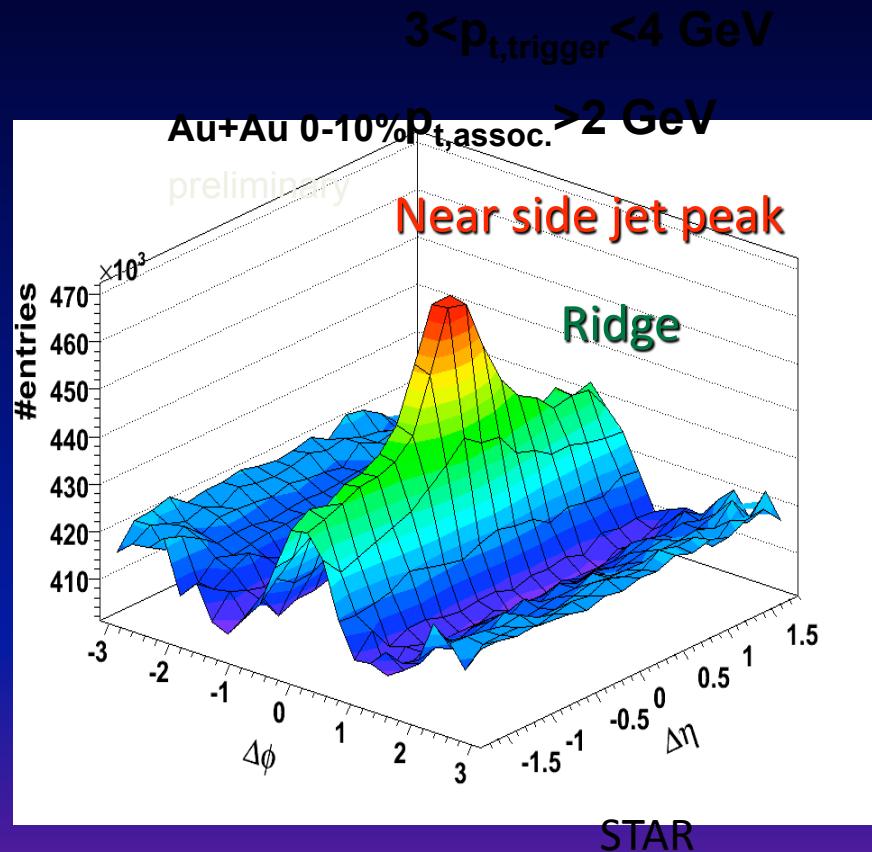
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# Phenomena

❖ Nuclear modification factors

❖ Jets structure

- Azimuthal angle
- 3 particle correlations
- $\Delta\eta$  and  $\Delta\phi$  : Ridge



# Phenomena

❖ Nuclear modification factors ☺

❖ Jets structure ☹

- Azimuthal angle
- 3 particle correlations
- $\Delta \eta$  and  $\Delta \phi$



Renk, Rupper, Nonaka, Bass, PRC75,031902(R),2007

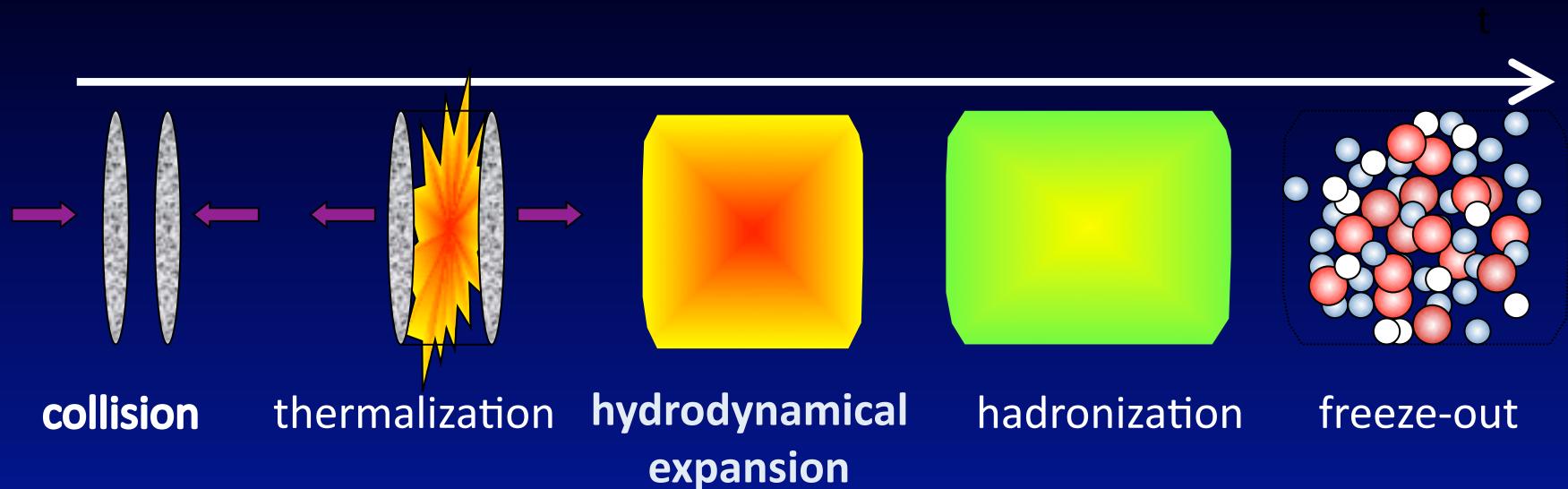
Majumder, Nonaka, Bass, PRC76,041902(R),2007

Qin,Rupper,Turbide,Gale,Nonaka,Bass,PRC76,064907(2007)

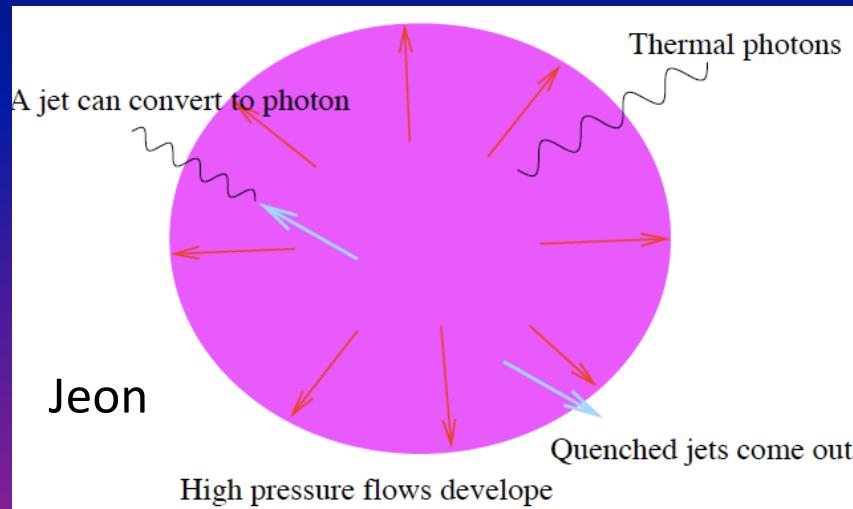
Bass,Gale,Majumder,Nonaka,Qin,Renk,Ruppert, PRC79,024901(2009)

# Relativistic Heavy Ion Collisions

## ❖ Schematic Sketch



Dynamics of  
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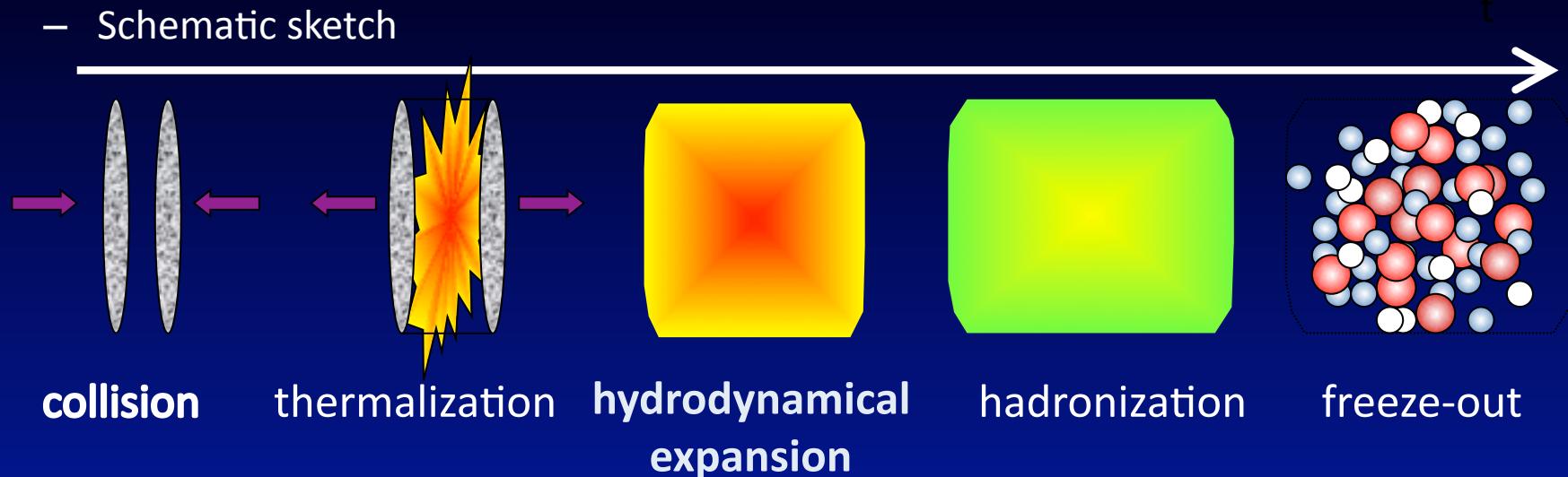


Jet quenching  
mechanism

# 3D Hydro + UrQMD

## ❖ Relativistic Heavy Ion Collision

- Schematic sketch



## ◎ 3D Hydro + UrQMD

### Full 3-d Hydrodynamics

- EoS : 1st order phase transition  
QGP + excluded volume model

### Hadronization

Cooper-Frye  
formula  
Monte Carlo

### UrQMD

final state  
interactions

$T_c$

$T_{SW}$

$t \text{ fm}/c$

# 3-D Hydrodynamic Model

- ❖ Relativistic hydrodynamic equation

$$\partial_\mu T^{\mu\nu} = 0$$

$T^{\mu\nu}$  : energy momentum tensor

- Baryon number conservation

$$\partial_\mu (n_B(T, \mu)) = 0$$

- ❖ Coordinates

$$(\tau, x, y, \eta) : \tau = \sqrt{t^2 - z^2}, \eta = \tanh^{-1} \left( \frac{z}{t} \right)$$

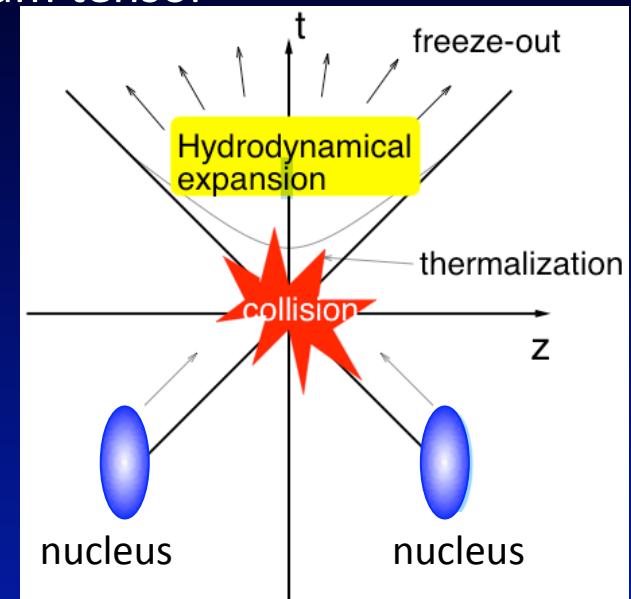
- ❖ Lagrangian hydrodynamics

- Tracing the adiabatic path of each volume element
- Effects of phase transition on observables
- Computational time
- Easy application to LHC

- ❖ Algorithm

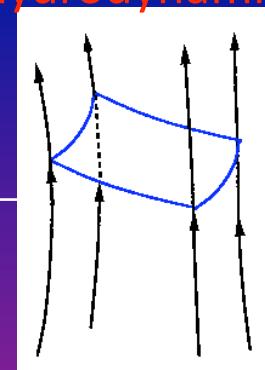
- Base on the conservation law

$$\partial_\mu (s(T, \mu) u^\mu) = 0, \partial_\mu (n_B(T, \mu) u^\mu) = 0$$



Lagrangian hydrodynamics

Flux of fluid



# Parameters

- ❖ Initial Conditions

  - Energy density

$$\epsilon(x, y, \eta) = \epsilon_{\max} W(x, y; b) H(\eta)$$

  - Baryon number density

$$n_B(x, y, \eta) = n_{B\max} W(x, y; b) H(\eta)$$

  - Parameters

$$\begin{cases} \tau_0 = 0.6 \text{ fm/c} \\ \epsilon_{\max} = 55 \text{ GeV/fm}^3, n_{B\max} = 0.15 \text{ fm}^{-3} \\ \eta_0 = 0.5, \sigma_\eta = 1.5 \end{cases}$$

  - Flow

$$v_L = \eta \text{ (Bjorken's solution); } v_T = 0$$

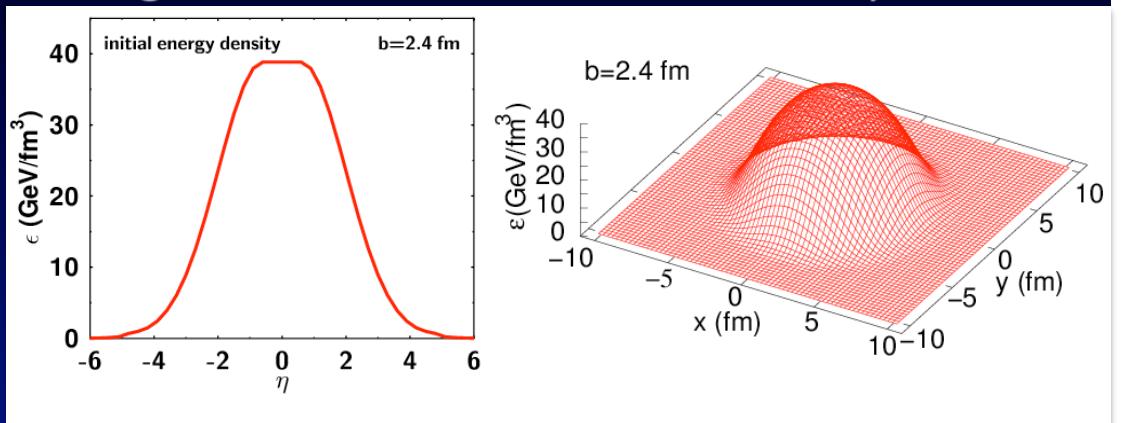
- ❖ Equation of State

1st order phase transition,  $T_c = 160 \text{ MeV}$

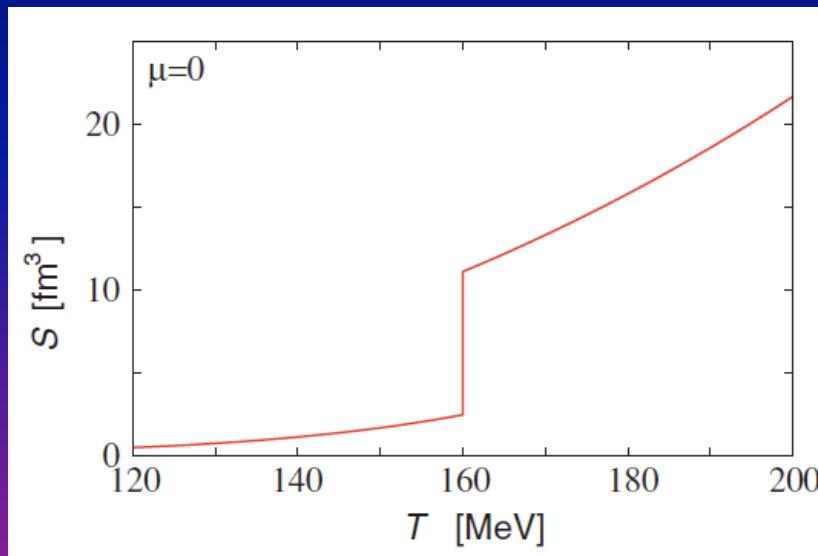
- ❖ Switching temperature

$$T_{\text{sw}} = 150 \text{ [MeV]}$$

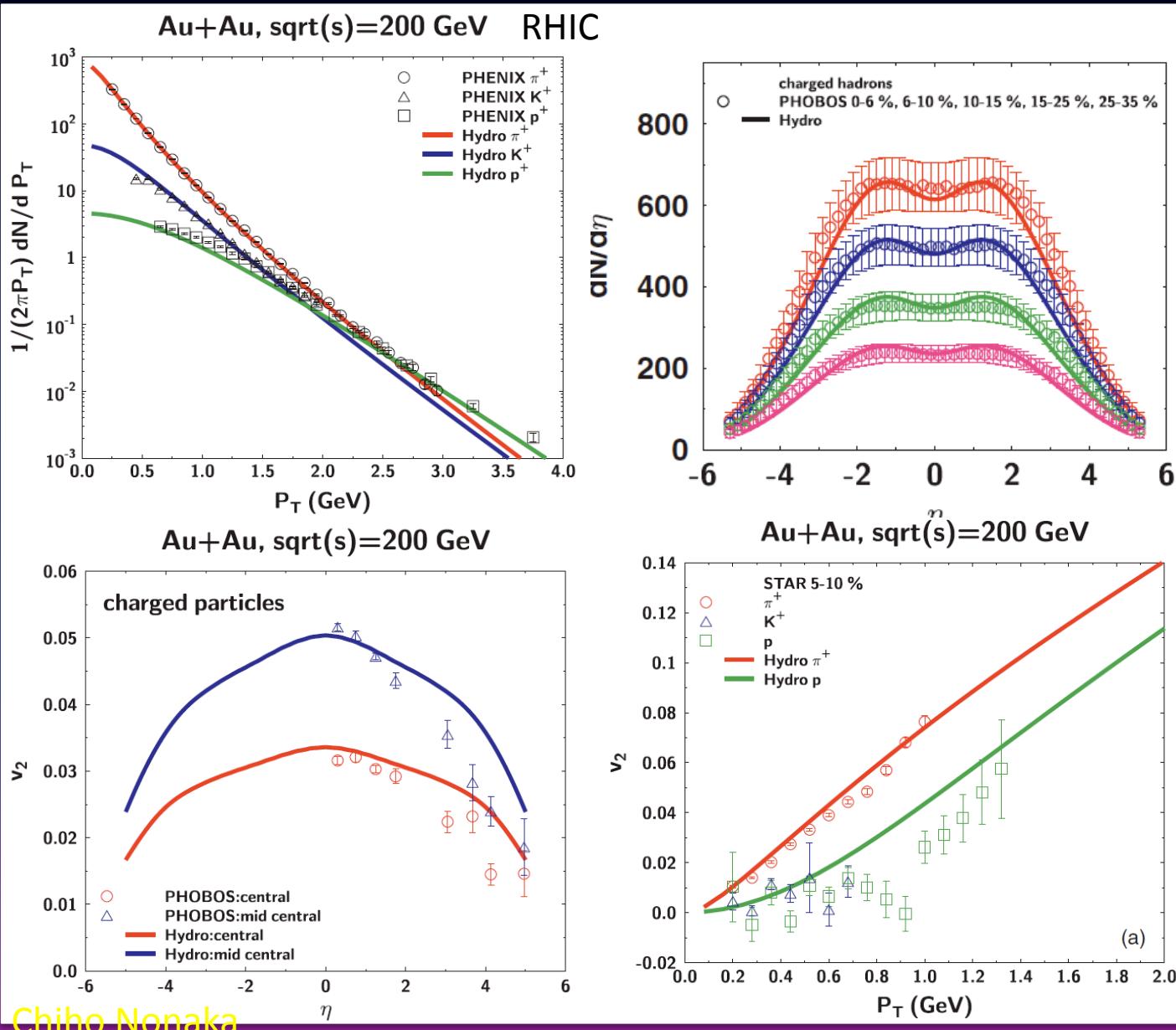
- longitudinal direction
- transverse plane



- Entropy density as a function of  $T$



# 3D Ideal Hydrodynamic Model



- Chemical equilibrium freezeout
- Final state interactions are neglected.

# Parameters

- Initial Conditions

  - Energy density

$$\epsilon(x, y, \eta) = \epsilon_{\max} W(x, y; b) H(\eta)$$

  - Baryon number density

$$n_B(x, y, \eta) = n_{B\max} W(x, y; b) H(\eta)$$

  - Parameters

$$\begin{cases} \tau_0 = 0.6 \text{ fm/c} \\ \epsilon_{\max} = 40 \text{ GeV/fm}^3, n_{B\max} = 0.15 \text{ fm}^{-3} \\ \eta_0 = 0.5, \sigma_\eta = 1.5 \end{cases}$$

  - Flow

$$v_L = \eta \text{ (Bjorken's solution); } v_T = 0$$

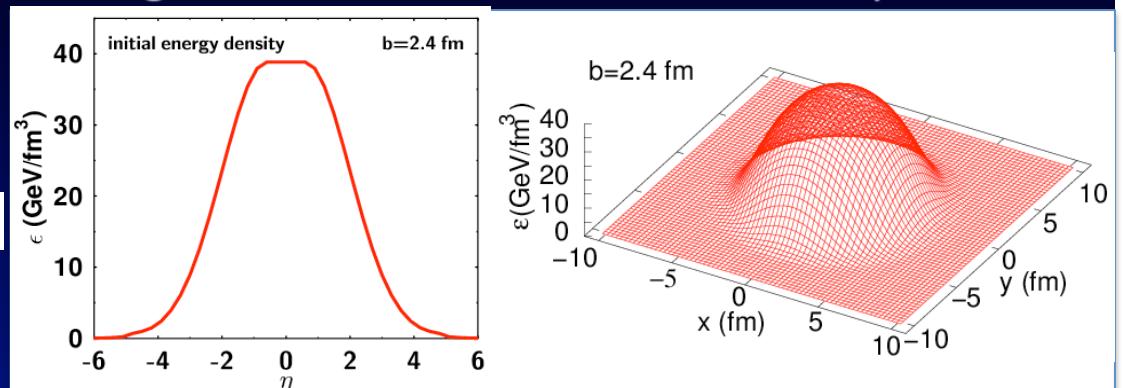
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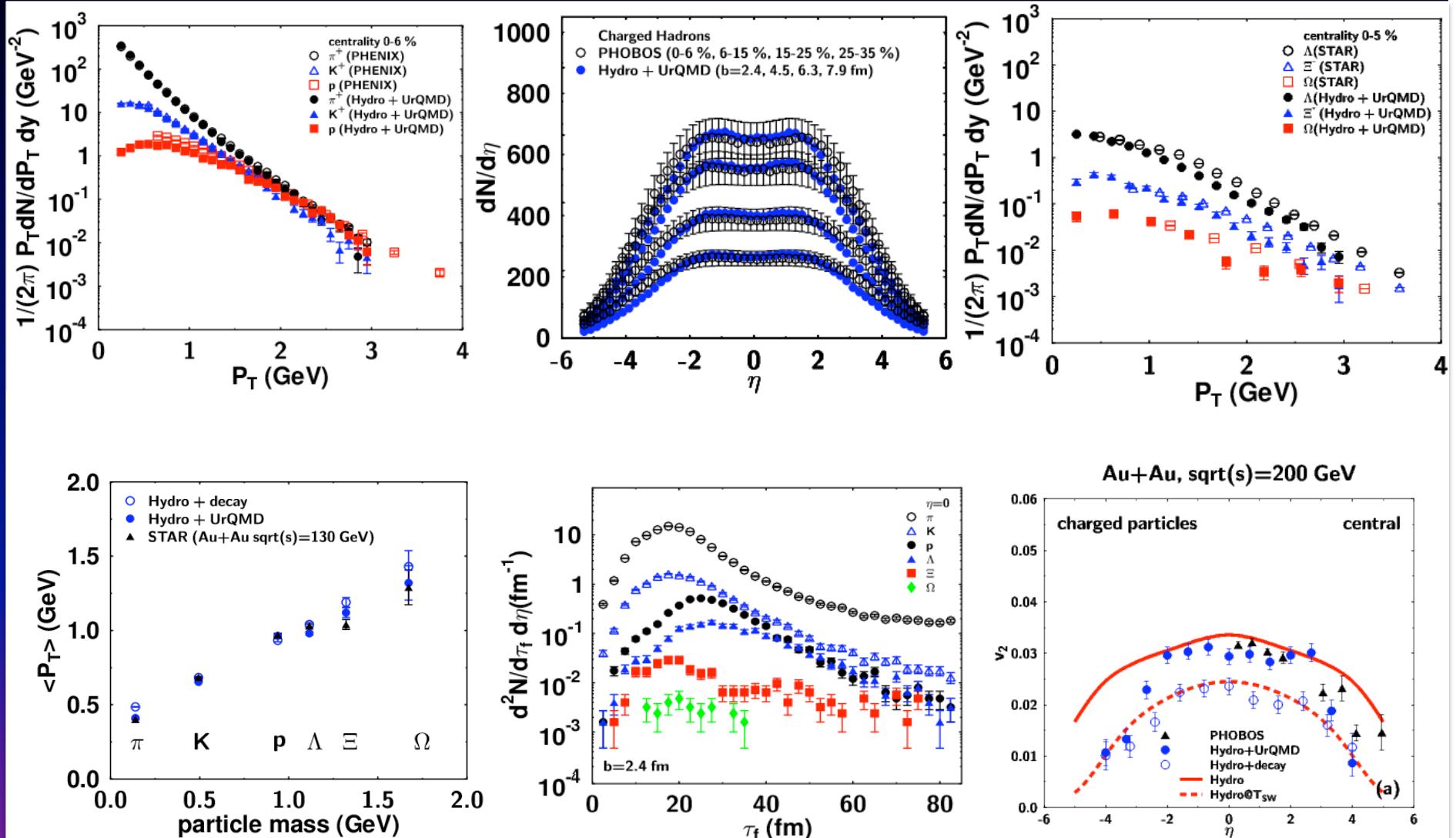
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- longitudinal direction
- transverse plane



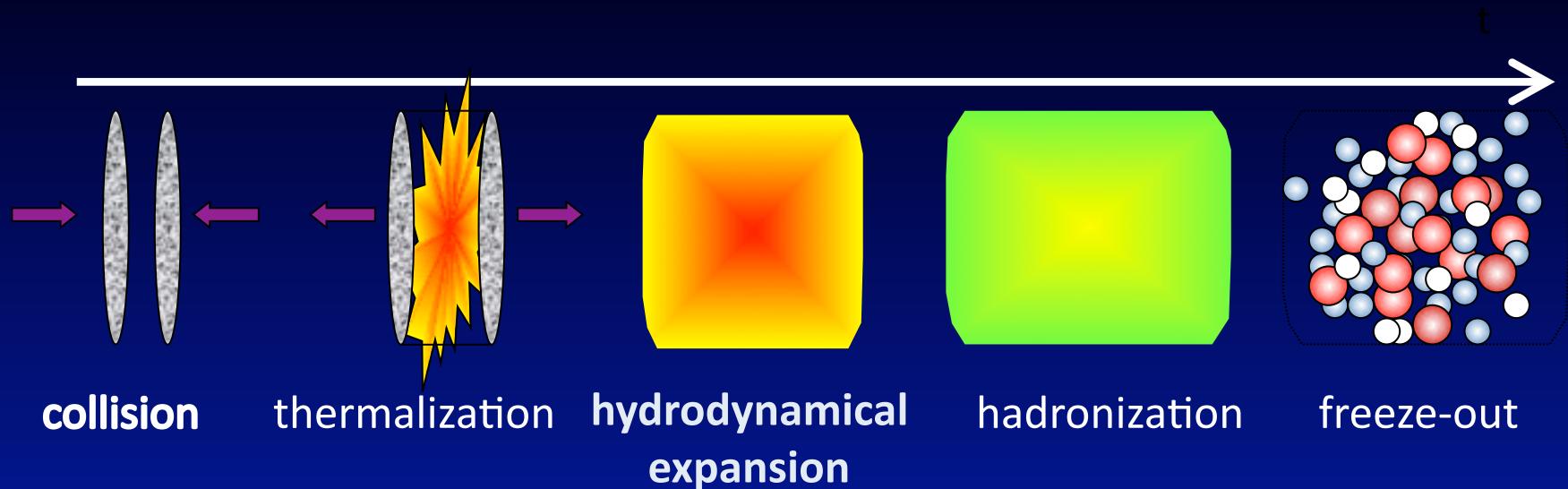
	hydro	Hydro+ UrQMD
$\tau_0(\text{fm})$	0.6	0.6
$\epsilon_{\max}(\text{GeV/fm}^3)$	55	40
$n_{B\max}(\text{fm}^{-3})$	0.15	0.15
$\eta_0, \sigma_\eta$	0.5, 1.5	0.5, 1.5

# 3D Ideal Hydro+UrQMD

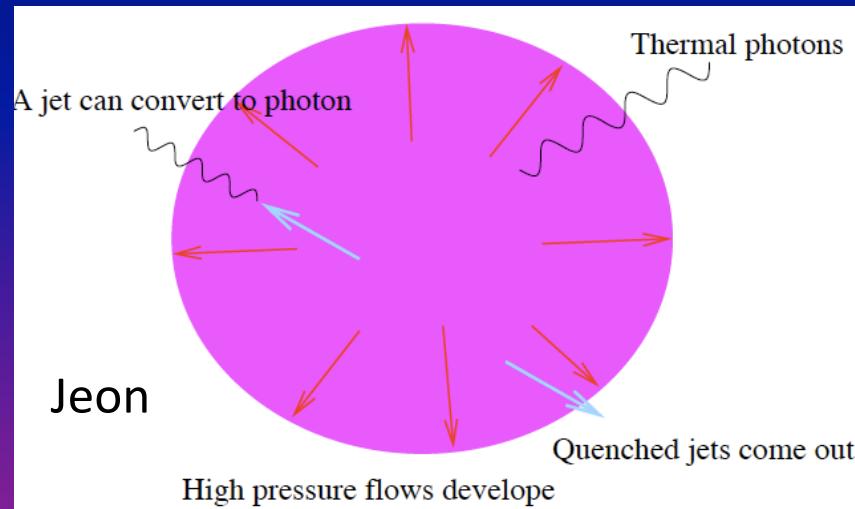


# Relativistic Heavy Ion Collisions

## ❖ Schematic Sketch



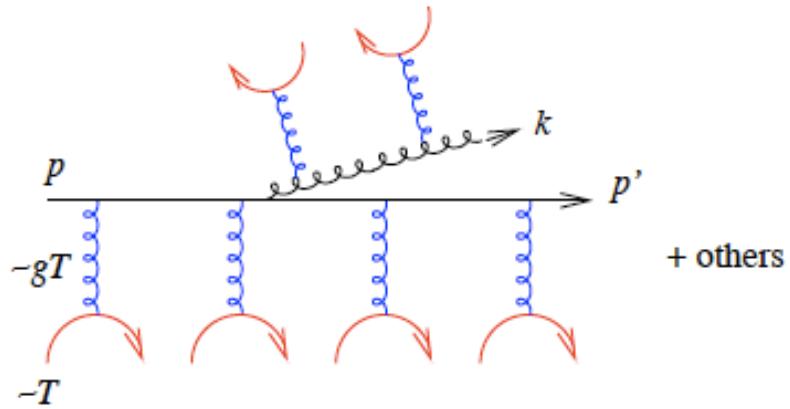
Dynamics of  
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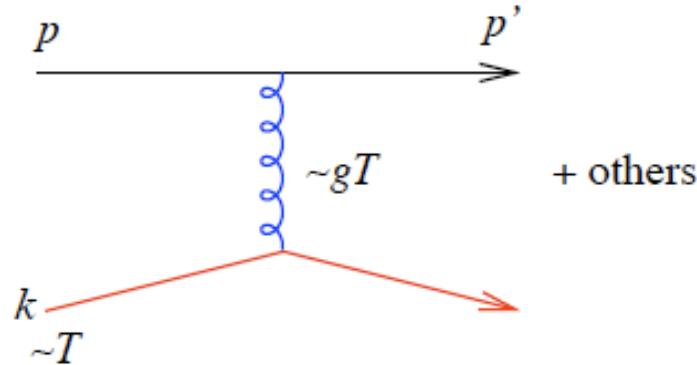
Jet quenching  
mechanism

# Energy Loss

- QGP makes jets lose energy
  - Radiational (Inelastic)



- Elastic



QGP?

Jeon@Nagoya

# Application of Hydro

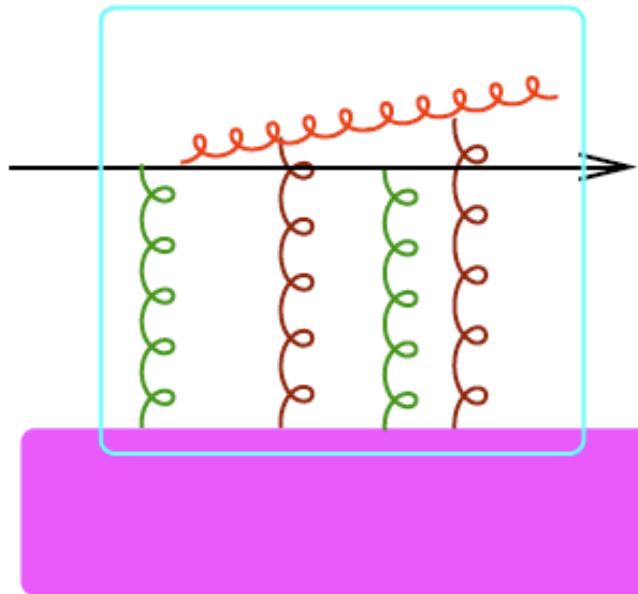
- ❖ Interactions between jets and medium

- Medium  $\leftarrow$  Hydrodynamic Model

- ❖ Systematic Comparison of Jet Energy-Loss Scheme

- BDMPS/ASW: path integral approach to the opacity expansion
  - Higher Twist (HT) soft sector : Hydro
  - Arnold-Moor-Yaffe (AMY) : finite temperature field theory approach
  - GLV: reaction operator approach to the opacity expansion  
Hirano and Nara, PRC69,034908(2004)

# Calculation Scheme



First calculate the *local* radiation rate  $\frac{dN_g}{d\omega dt}$

The magenta box:

- QGP medium characterized by  $T, g_s$  – AMY, DGLV
- Static medium characterized by  $\mu, l_{\text{mfp}}$  – BDMPS-Z, GLV, AWS, ...
- General nuclear medium with short color correlation – HT

Jeon@QM2009



# Hadron Production

$$\frac{d^2\sigma^h}{dyd^2p_T} = \frac{1}{\pi} \int dx_a \int dx_b G_a^A(x_a) G_b^B(x_b) \frac{d\sigma_{ab \rightarrow cX}}{d\hat{t}} \frac{\tilde{D}_c(z)}{z}$$

same initial state

$G(x)$  : parton distribution function: CTEQ5

Vacuum fragmentation functions: KKP, AKP

different in each energy loss scheme : ASW, HT, AMY

$\tilde{D}_c(z)$ : medium modified fragmentation function

# Energy Loss in Medium

- ❖ Information of medium: thermodynamic values, velocity

← Hydrodynamic Models

- ❖ Transport coefficients in each energy loss scheme

- BDMPS/ASW

$$\hat{q}(\xi) = K \cdot 2 \cdot \varepsilon^{\frac{3}{4}}(\xi) \quad \xi: \text{trajectory of jets}$$

- Higher Twist

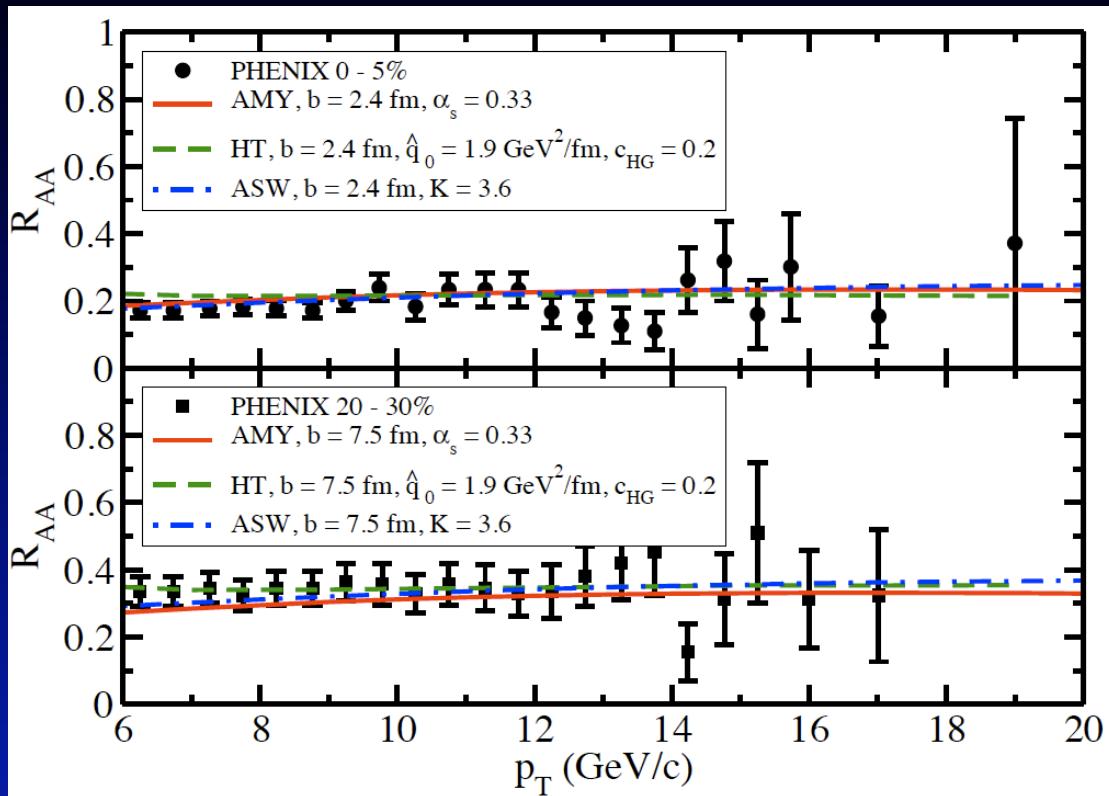
$$\hat{q}(\vec{r}, \tau) = \hat{q}_0 \frac{\gamma(\vec{r}, \tau) T^3(\vec{r}, \tau)}{T_0^3} [R_{QGP}(\vec{r}, \tau) + c_{HG}(1 - R_{QGP}(\vec{r}, \tau))] \quad R_{QGP}: \text{ratio of QGP phase}$$

$q_0$  at initial time( 0.6 fm/c),  $c_{HG}$  hadron phase

- AMY:  $\alpha_s$

$$\hat{q}(\vec{r}, \tau) = \frac{C_A g^2 T(\vec{r}, \tau) m_D^2}{2\pi} \ln \frac{q_\perp^{\max}}{m_D}$$

# Nuclear Modification Factors



- Predictions:  
 $p_T$  dependence,  
centrality dependence
- Very small difference  
More sophisticated  
observables are needed.

Parameters: fixed in central collisions

ASW	HT	AMY
$K=3.5$	$q_0=1.9 \text{ GeV}^2/\text{fm}$	$\alpha_s=0.33$

# Scaling with the Medium

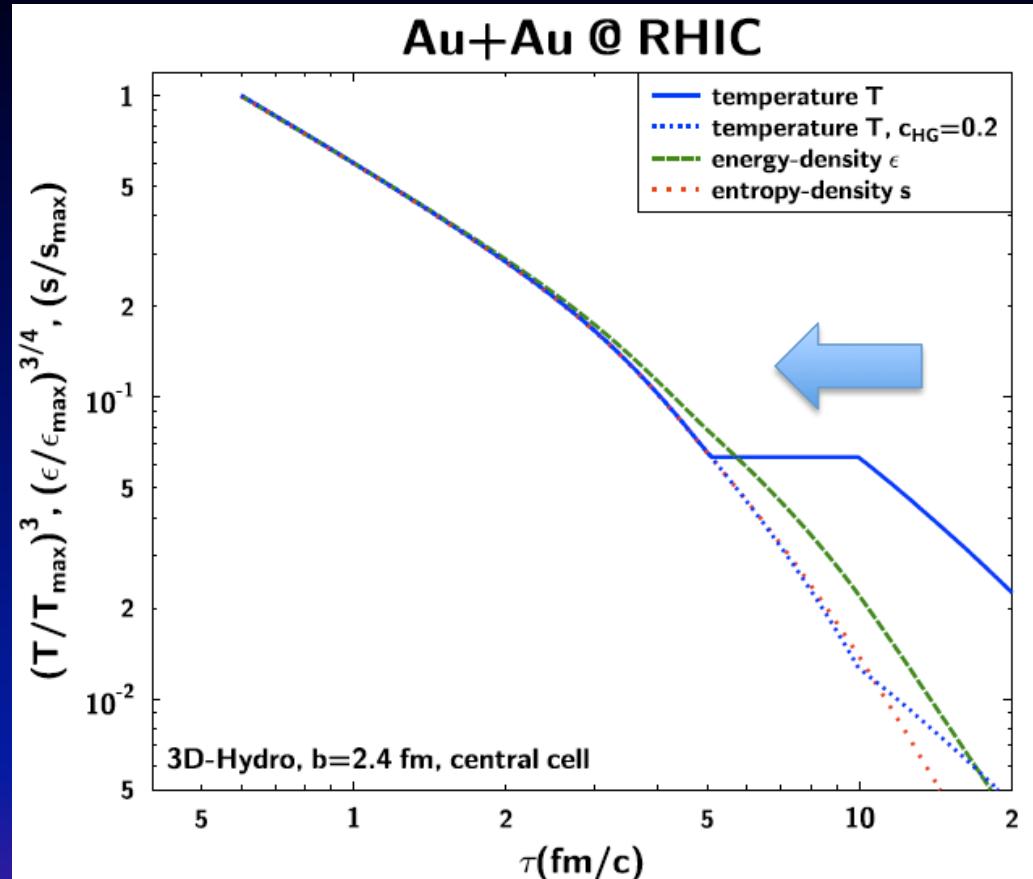
Possible choices of scaling

$$\hat{q} \sim T^3 \quad \hat{q} \sim \epsilon^{3/4} \quad \hat{q} \sim s$$

$T, \epsilon, s$ : Information of medium  
Hydrodynamic model &  
Equation of states

- Bjorken expansion with Ideal QGP
  - Identical results
- Hydro with realistic equation of state
  - different time dependence

realistic dynamical model,  
proper medium scaling



- Choice of  $c_{HG}=0.2$  mimics scaling with entropy density

PRC79,024901(2009)

# Quantitative Comparison

$$\hat{q}(\xi) = \hat{q}_0 \cdot \Gamma(\xi)$$

$\xi$ : trajectory of jets in medium

$\hat{q}_0$ : initial maximum value

-BDMPS/ASW

$$\hat{q}(\xi) = K \cdot 2 \cdot \epsilon^{\frac{3}{4}}(\xi)$$

$\hat{q}(\vec{r}, \tau)$ scales as	ASW $\hat{q}_0$	HT $\hat{q}_0$	AMY $\hat{q}_0$
$T(\vec{r}, \tau)$	$10 \text{ GeV}^2/\text{fm}$	$2.3 \text{ GeV}^2/\text{fm}$	$4.1 \text{ GeV}^2/\text{fm}$
$\epsilon^{3/4}(\vec{r}, \tau)$	$18.5 \text{ GeV}^2/\text{fm}$	$4.5 \text{ GeV}^2/\text{fm}$	
$s(\vec{r}, \tau)$		$4.3 \text{ GeV}^2/\text{fm}$	

-Higher Twist

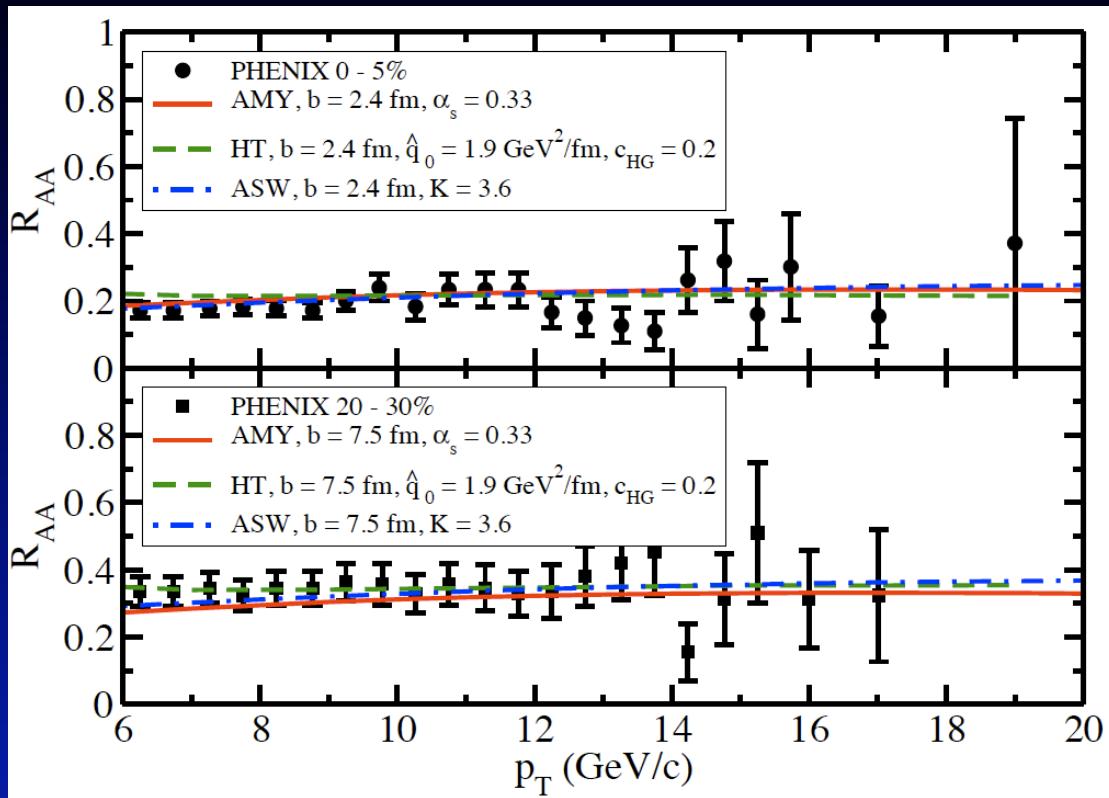
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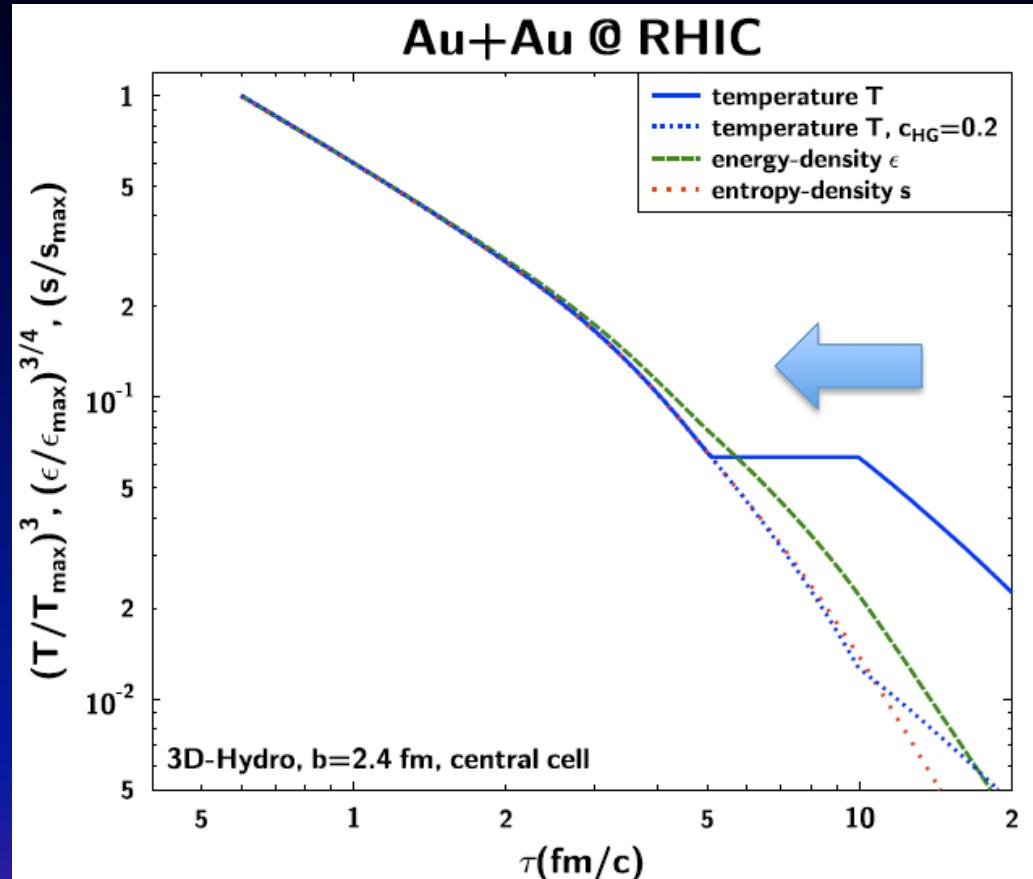
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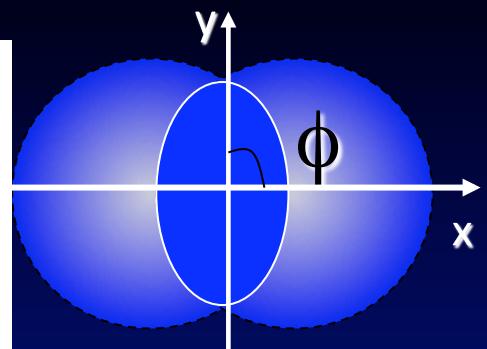
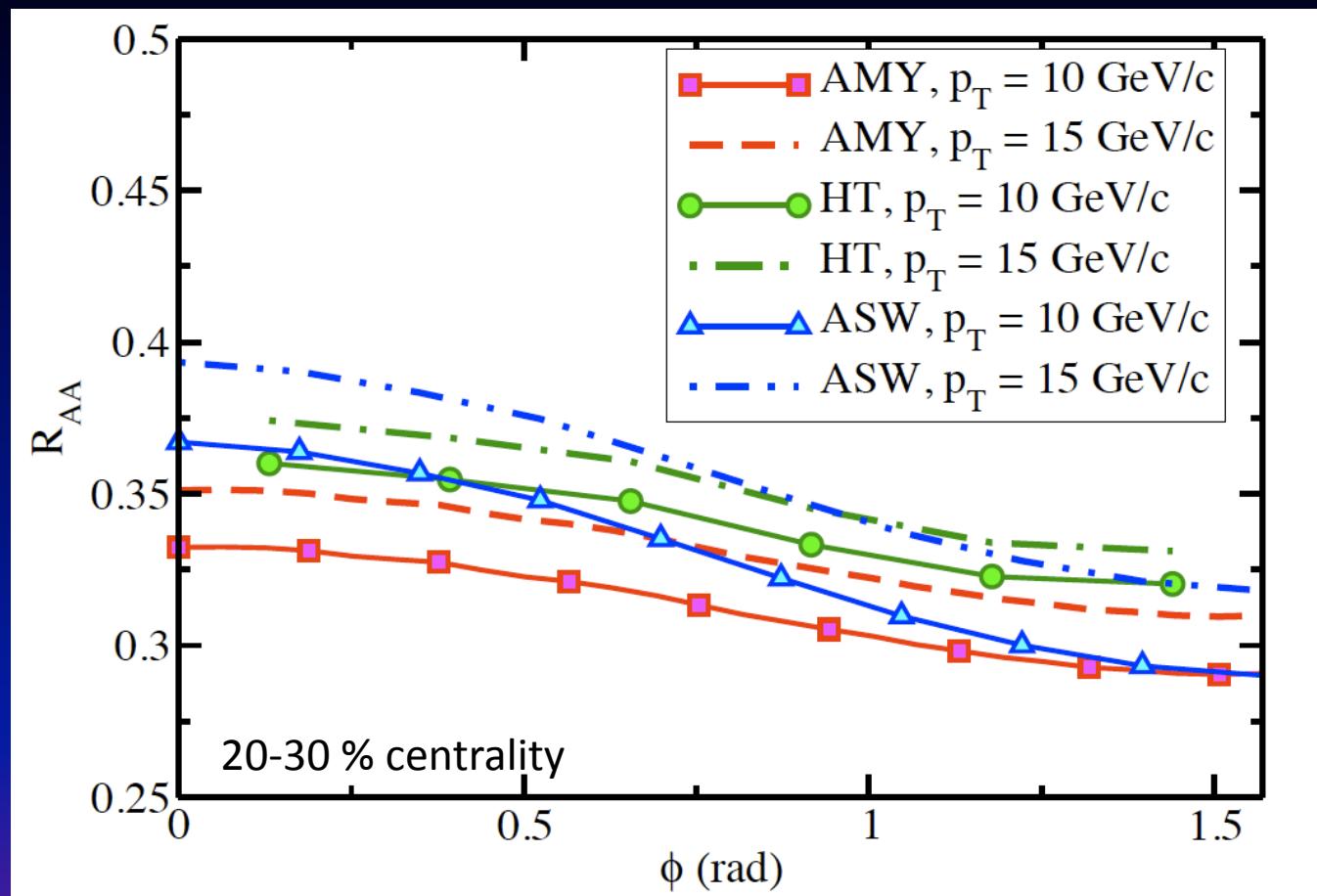
realistic dynamical model,  
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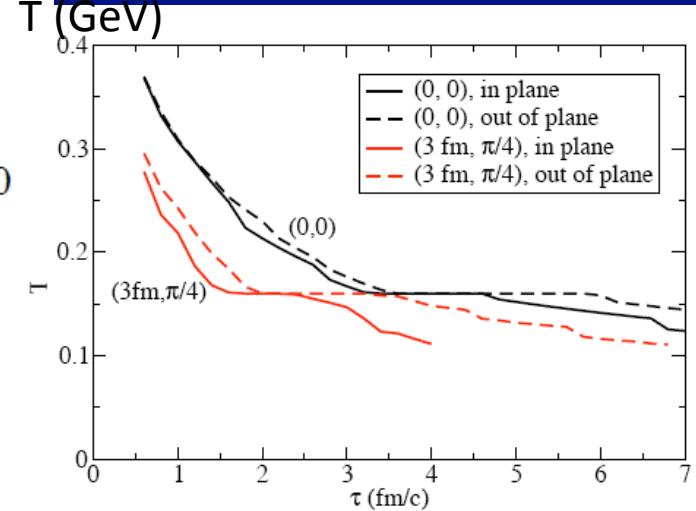
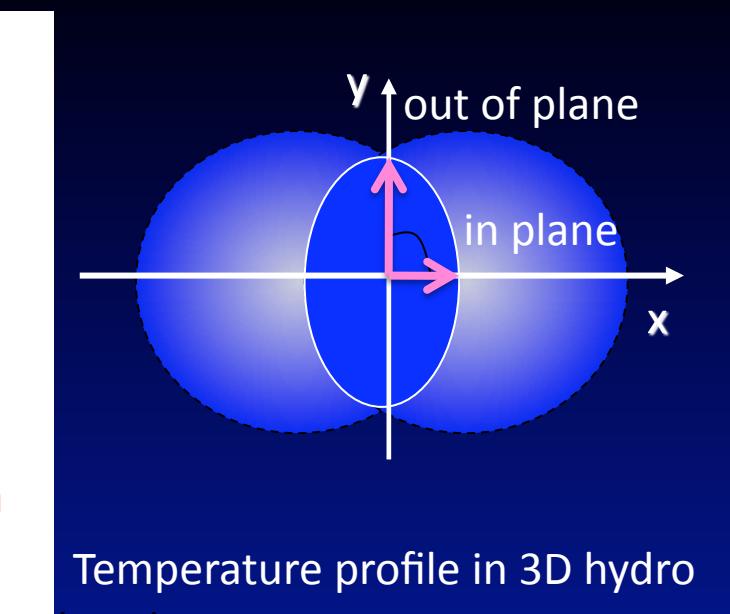
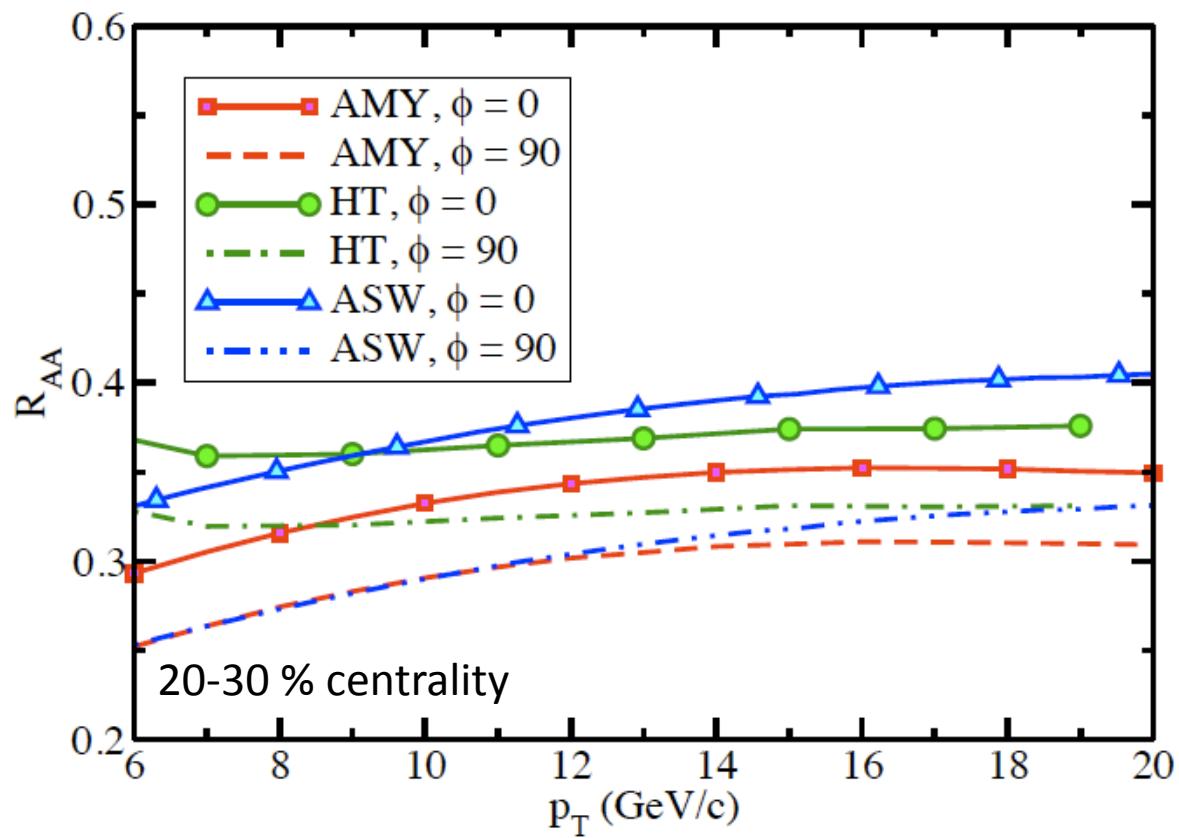
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PRC79,024901(2009)

# Azimuthal angle dependence

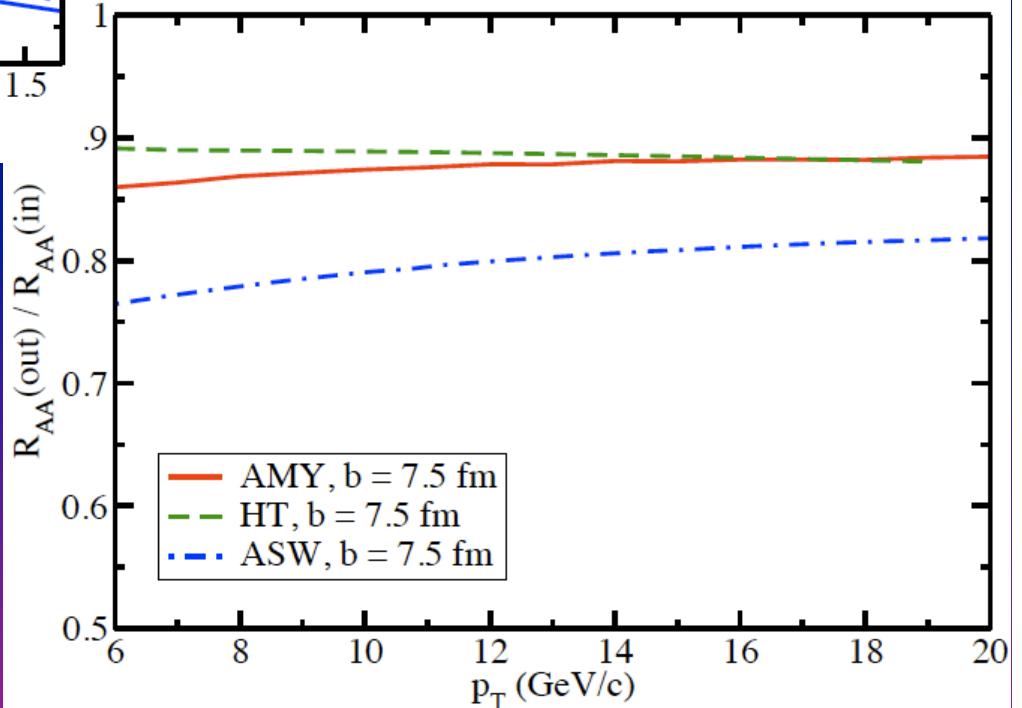
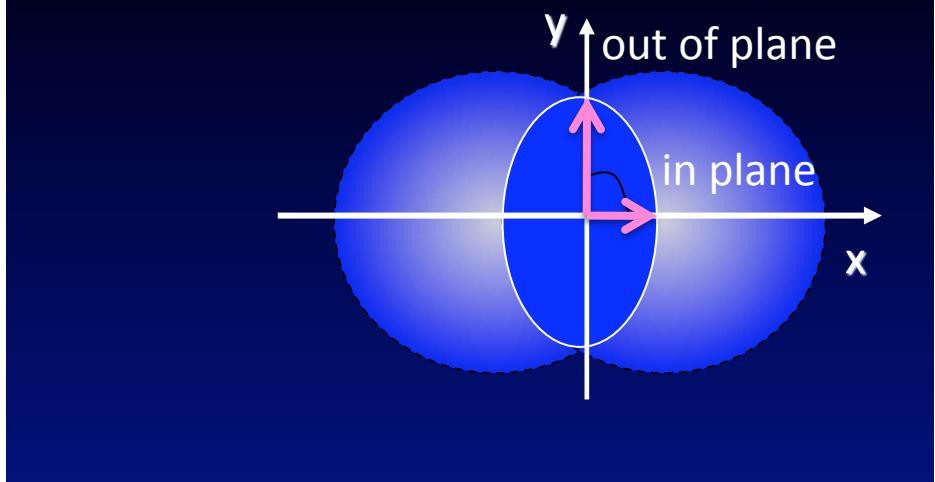
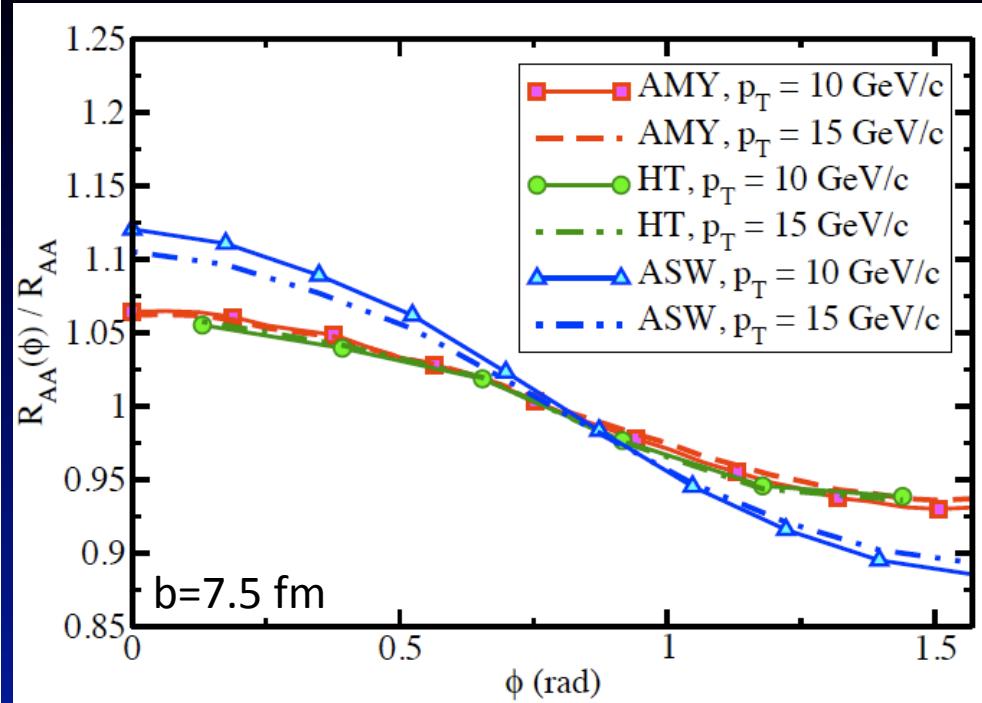


# $R_{AA}$ for In/Out of plane



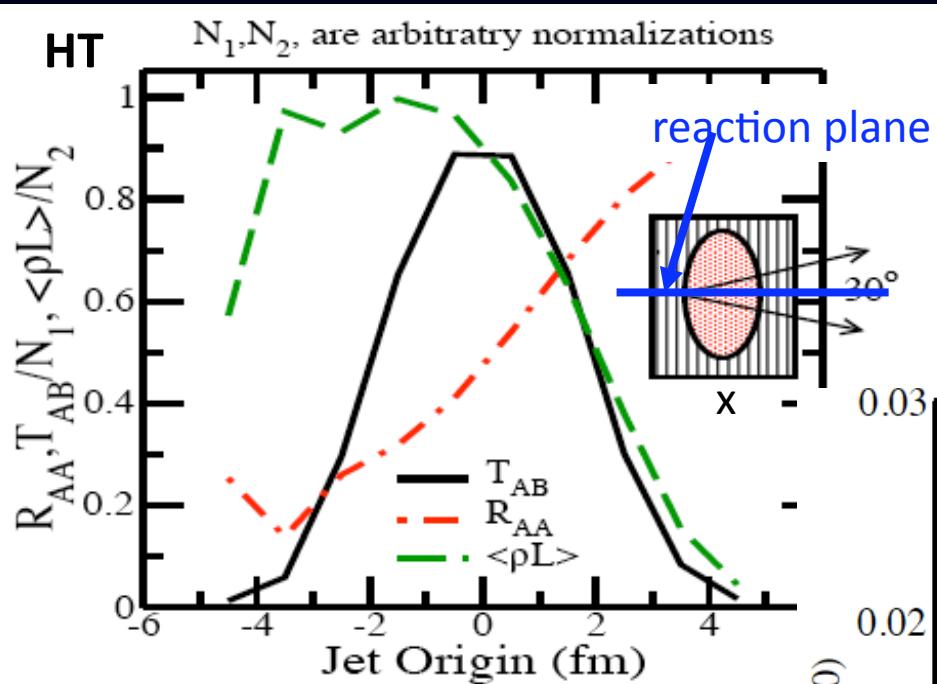
- AMY & HT: same azimuthal spread, but difference in magnitude

# Azimuthal Spread

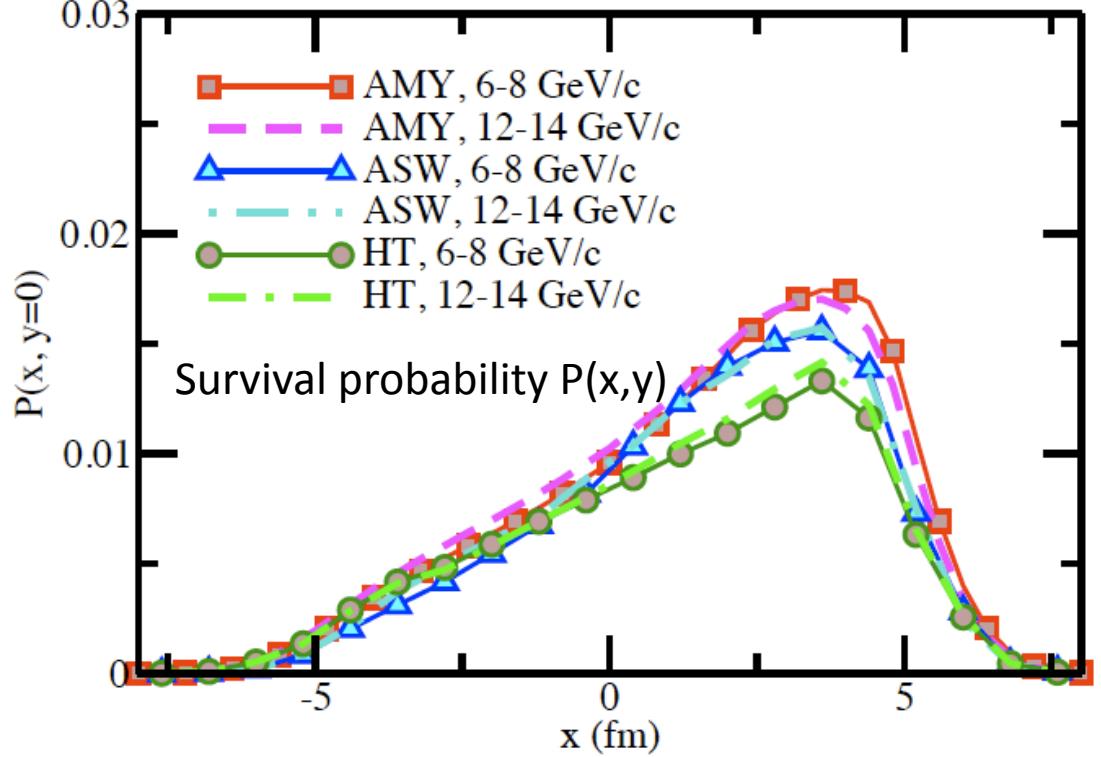


- ASW shows a significantly stronger azimuthal dependence of  $R_{AA}$  than AMY & HT

# Nuclear Modification Factor



- Three approaches agree with each other  
→ Same suppression factor



$R_{AA}$  is anticorrelated with  $\langle \rho L \rangle$

# Summary

- ❖ Soft sector: 3D Hydro + UrQMD Model
  - Success at RHIC:  $P_T$  spectra, rapidity distribution, elliptic flow
- ❖ Jets in medium
  - Jet quenching mechanisms: BDMPS /ASW, higher twist and AMY
  - Nuclear modification factors
    - Transport coefficients

# TECHQM

❖ [https://wiki.bnl.gov/TECHQM/index.php/Main\\_Page](https://wiki.bnl.gov/TECHQM/index.php/Main_Page)



**TECHQM**

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## TECHQM:About

### TECHQM: Theory-Experiment Collaboration for Hot QCD Matter [\[edit\]](#)

The goal of TECHQM is to further the understanding of hot QCD matter through detailed, quantitative analysis of heavy ion collision experimental data and theory, together with the dynamical modeling which connects them.

The complex, dynamic nature of a heavy ion collision dictates the need for extensive theoretical modeling as the bridge between experimental observations and underlying properties of the hot QCD Matter. While good progress has been made in this area, providing essential support for interpretation of RHIC data on flow and jet quenching, there are still significant conceptual and modeling uncertainties which limit the accuracy with which conclusions can be drawn about the properties of QCD matter.

In the view of the TECHQM working group, elucidation and reduction of these uncertainties requires coherent, sustained, collaborative effort of experts in all stages of a heavy ion collision. A collaborative effort of theorists and experimentalists, aimed at systematic validation of different approaches to the modeling of heavy ion collisions, will be able to go significantly beyond the scope achievable by individual research groups, which usually concentrate on the development of models for specific collision stages. This is not an issue for the RHIC or LHC communities in isolation in our view, full understanding of the physics at both facilities will require a unified approach, to compare and contrast their results within common calculational frameworks.

The first TECHQM meeting was held at Brookhaven National Laboratory, May 6-7, 2008: <http://www.bnl.gov/techqm/default.asp>

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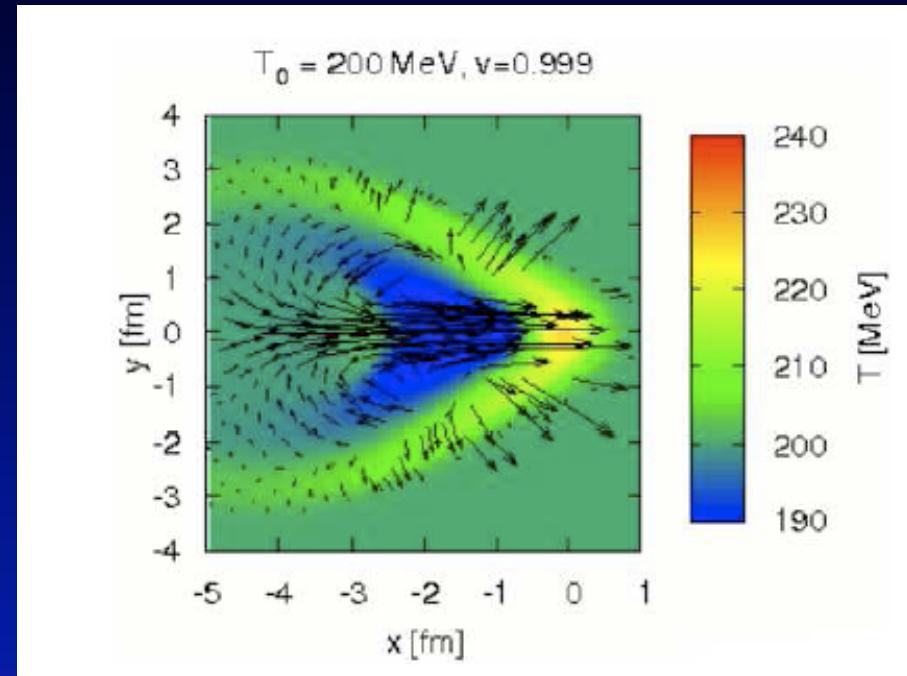
Working Groups: partonic energy loss  
bulk evolution

# Event Generators

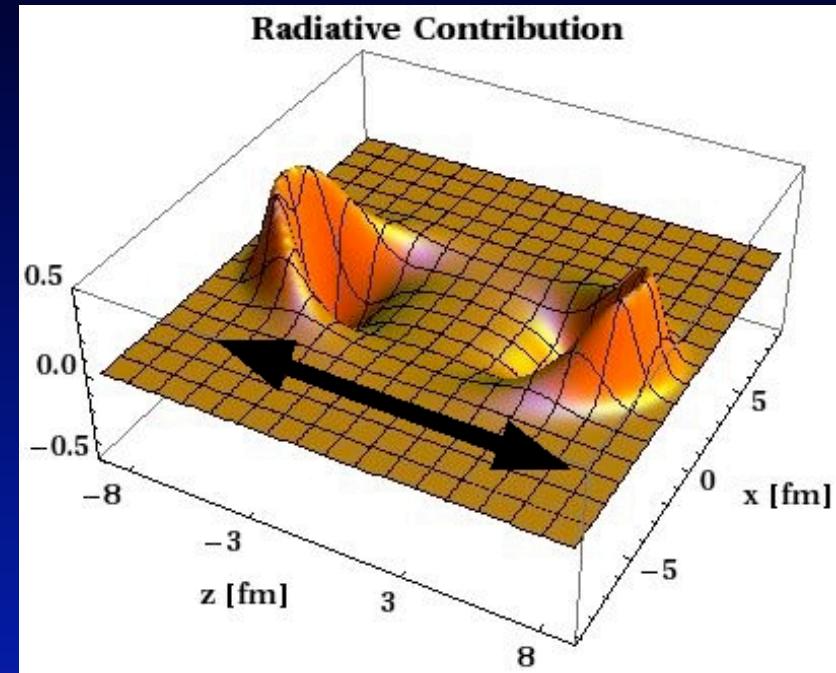
- YaJEM – T. Renk, Tues.Plenary  
(**Y**et **a**nother **J**et **E**nergy loss **M**odel)
- JEWEL – Zapp, Ingelman, Rothsman, Stachel, Wiedemann – K.C. Zapp, Tues.1A  
(**J**et **E**volution **W**ith **E**nergy **L**oss)
- Q-PYTHIA – Armesto, Salgado, Cunqueiro, Corcella – C. Salgado, Tues.2A
- PQM – Dainese, Loizides, Paić  
(**P**arton **Q**uenching **M**odel)
- PYQUEN/HYDJET – Lokhtin, Petrushanko, Snigirev, Teplov, Mailinina, Arsene, Tywoniuk
- MARTINI – McGill-AMY  
(**M**odular **A**lgorithm for **R**elativistic **T**reatment of **H**eavy **I**oN **I**nteractions)

# Mach Cone

- ❖ Interactions between medium and jets



B.Betz et al. 0812.4401

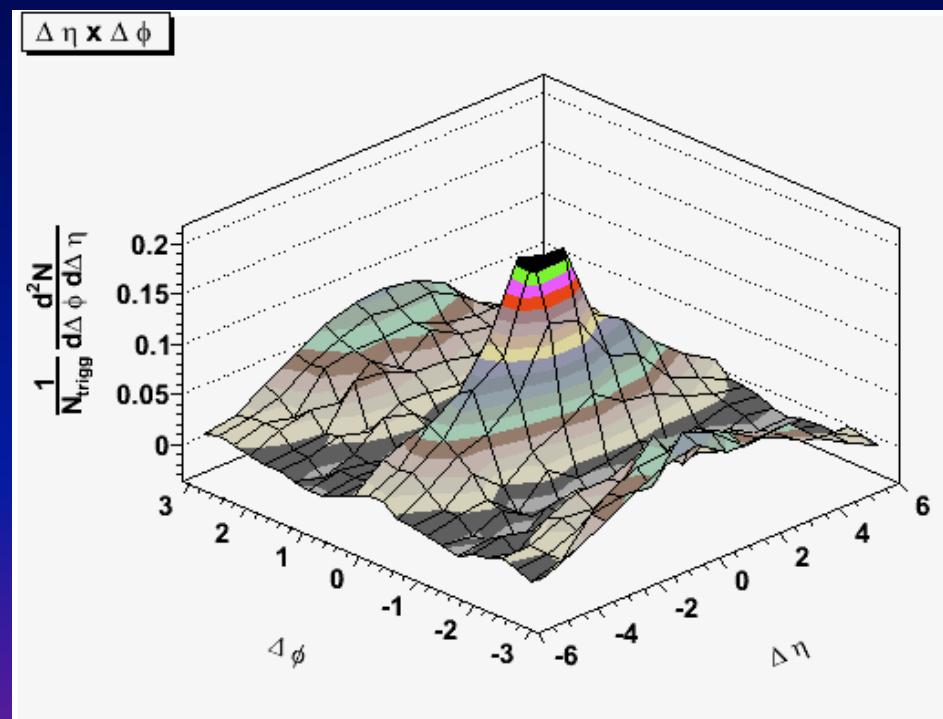


Neufeld and Mueller 0902.2950

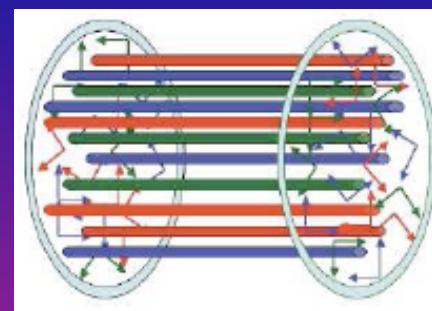
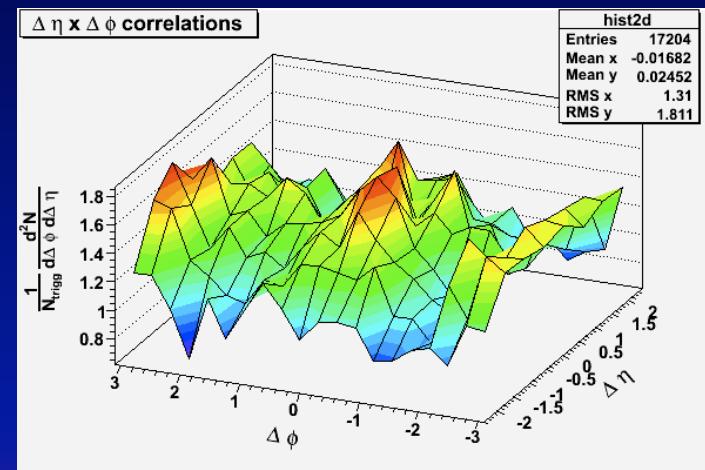
AdS/CFT

# Possible Solution to Ridge

❖ Brazil group



Averaged initial conditions



Flux tube  
+  
fluctuations

# Challenge

## Theory:

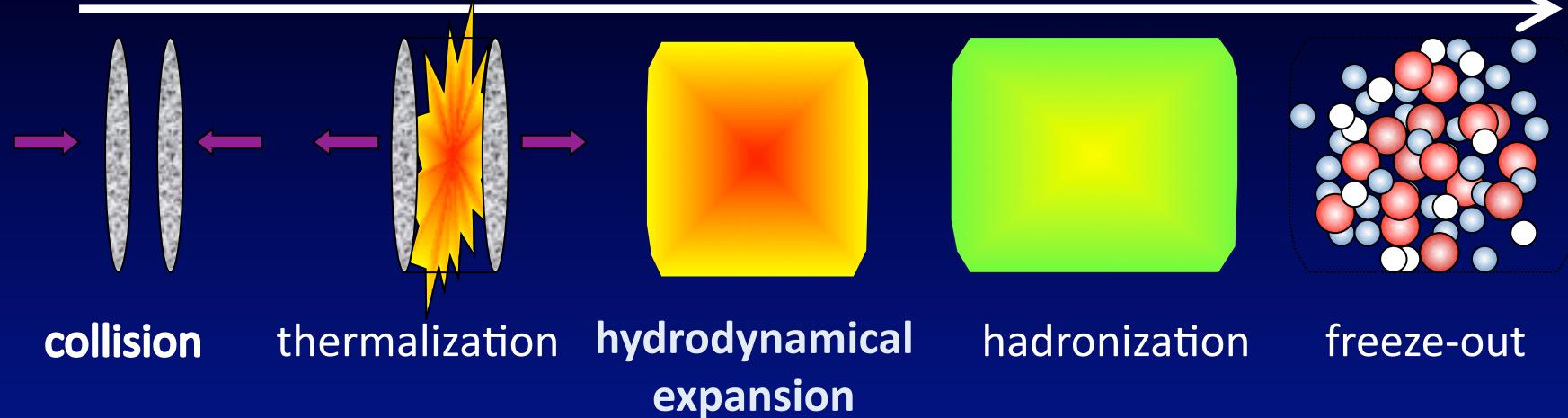
- ❖ Towards quantitative calculations
  - Dynamical model
  - Jet quenching mechanism

## Phenomena:

- ❖ Azimuthal angle distribution Esumi-san's talk!
  - Reaction plane dependence?
  - Elliptic flow?
- ❖ Collisions energy dependence?

# Toward More Realistic Dynamical Model

❖ Based on hydrodynamic models: Multi Module Modeling



## Initial Conditions

- Event by event fluctuation
- elliptic flow vs  $N_{\text{part}}$
- Hirano and Nara
- Ridge
- Brazil group

## Hydrodynamics

- Viscosity
- shear, bulk
- Equation of state
- QCD critical point?

## Freezeout process

- Hadronization – Recombination
- Final state interactions