

流体、バルク、フロー

Kobayashi-Maskawa Institute
for the Origin of Particles and the Universe
Department of Physics, Nagoya University
Duke University

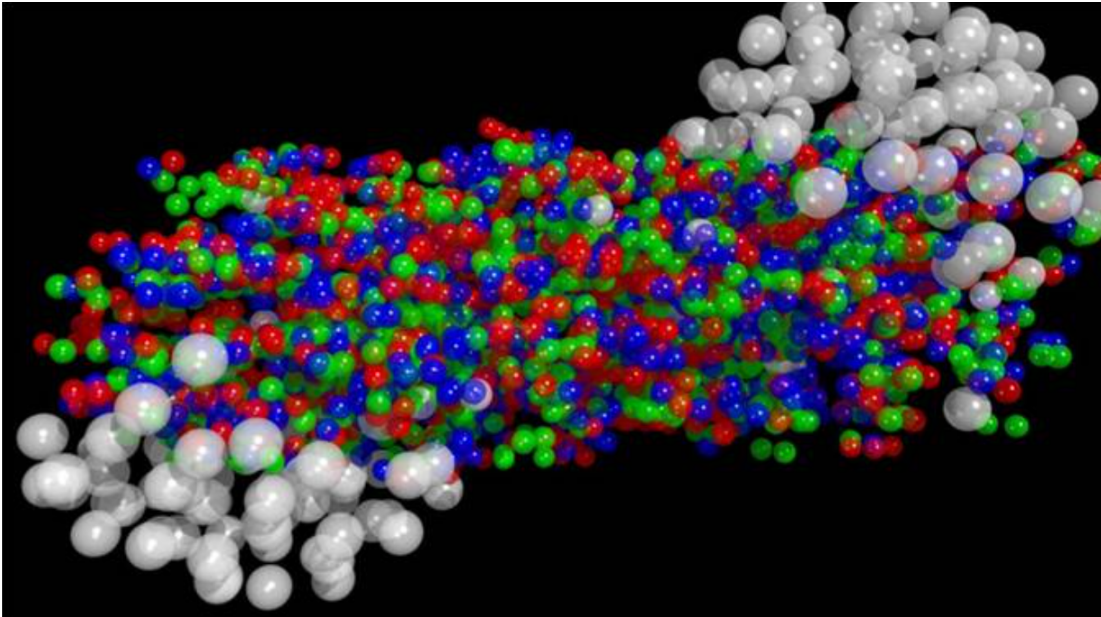


Kobayashi-Maskawa Institute
for the Origin of Particles and the Universe

Chiho NONAKA

April 8, 2017@Nagoya

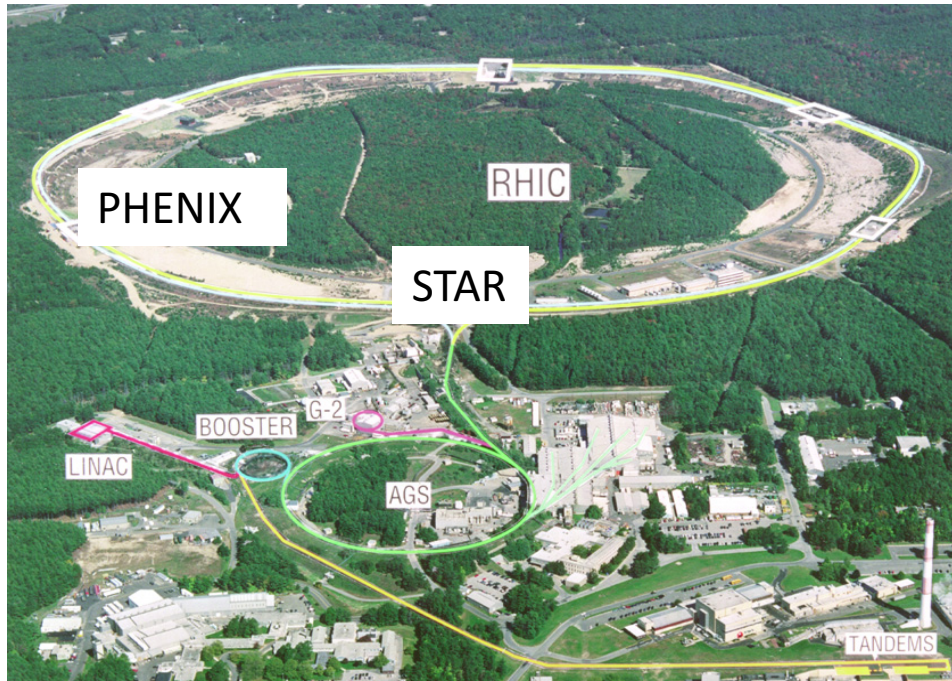
QM2017@Chicago



XXVI international conference
on ultrarelativistic heavy-ion
collisions

- From February 5 to February 11
- More than 700 participants!
- 37 plenary talks and 176 parallel talks + ~300 posters

Heavy Ion Collisions



RHIC@BNL

Large Hadron Collider@CERN



Tools & Physical Observables

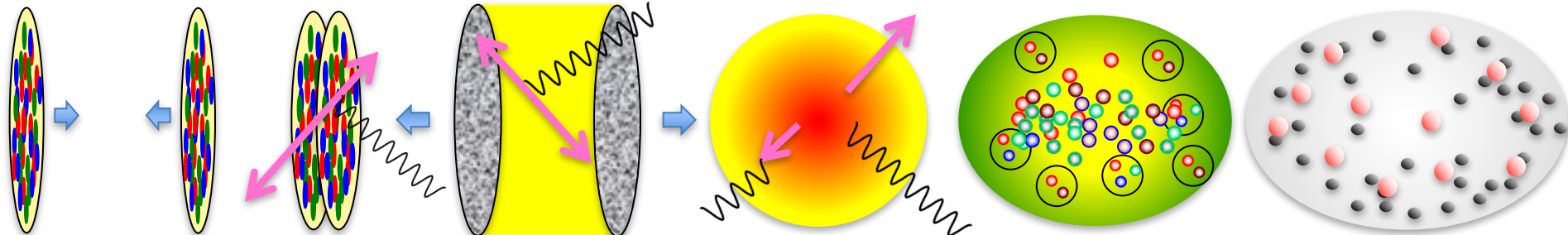
collisions

thermalization

hydro

hadronization

freezeout



Tools

hydrodynamics

partons event generator hadrons

Color Glass Condensate

recombination
fragmentation

4 田屋: 初期過程

3 本郷: カイラル磁気・渦効果、理論の発展

statistical model

Physical observables

6 山口

photons/leptons

1 野中・2 中込

bulk property

5 坂井

Jets

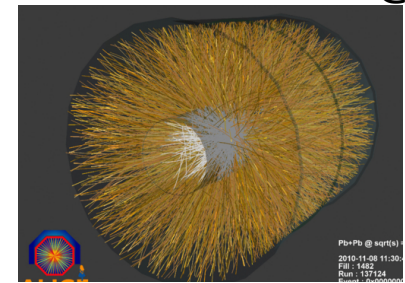
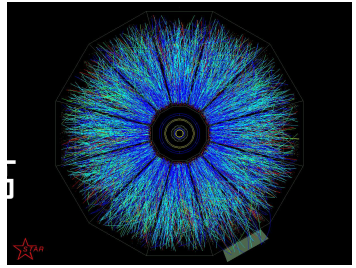
7 渡辺

heavy quarkonia

Heavy Ion Collisions@QM2017



STAR@RHIC



Au+Au(Beam Energy Scan)
7.7, 11.5, 19.8, 27, 39

p+p,
d+Au, He+Au
U+U, Au+Au,
200

Pb+Pb
2760
p+Pb
Pb+Pb
5020 GeV



Heavy Ion Collisions@QM2017

p+p, ?
d+Au, He+Au

p+p
p+Pb ?

Au+Au (Beam Energy Scan)
7.7, 11.5, 19.8, 27, 39 ?

U+U, Au+Au,
200

Pb+Pb
2760

Pb+Pb
5020 GeV

RHIC

LHC

$\sqrt{s_{NN}}$

流体模型

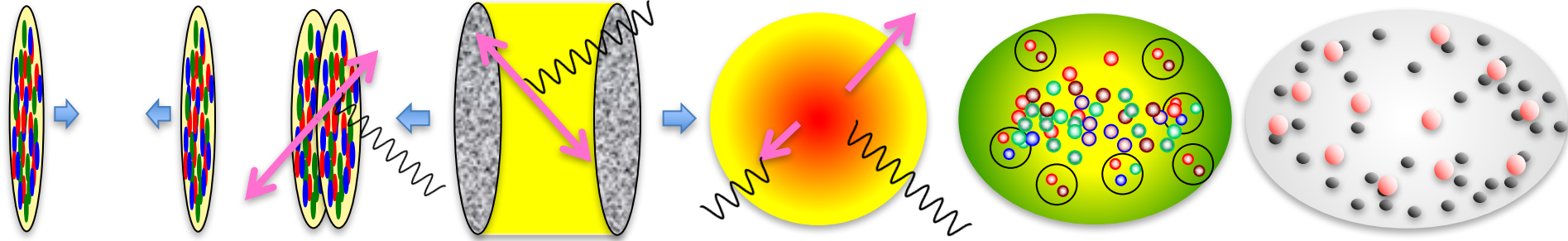
collisions

thermalization

hydro

hadronization

freezeout



Initial conditions

Hydrodynamics

Final state interactions

Fluctuations:
Glauber, KLN,
IP-Glasma...

QGP bulk property
EoS: lattice QCD
**Shear and bulk
viscosities**

Cooper-frye+decay
MC sampling
Hadron based event
generator

Hydrodynamic Model@QM17

Speaker	IC	Hydro	Particization	observables	system
Eskola	NLO pQCD + saturation	(2+1)-d, η	CF, decay, vis	v_n , correlation	Au+Au, Pb+Pb
Denicol	IP-Glasma	MUSIC, η, ζ	UrQMD	v_2, v_3	RHIC/LHC
Bernhard	TRENTO	(2+1)-d, η, ζ	UrQMD	Yield, $\langle P_T \rangle, v_n$	Pb+Pb
McDonald	IP-Glasma	MUSIC, η, ζ	UrQMD	Flow 全般	Pb+Pb
Gardim	NEXUS	SPHERIO	MC sampling	correlation	Au+Au
Luzum	NEXUS	SPHERIO	MC sampling	fluctuations	Au+Au
Sakai	MC-Glauber	Thermal fluc, η	JAM	factorization	Pb+Pb
Wang	AMPT	(3+1)-d, η	CF, decay	Λ , vorticity	Au+Au
Karpenko	UrQMD	(3+1)-d, η	UrQMD	Λ , vorticity	Au+Au(BES)
Auvinen	UrQMD	(3+1)-d, η	UrQMD	Yield, HBT, v_2	Au+Au(BES)
Shen	MC-Glauber+Lexus	MUSIC, η, κ	Hadron cascade	Yield	Au+Au(BES)
Moreland	TRENTO	(2+1)-d, η, ζ	UrQMD	Yield, v_n	P+Pb
Kawaguchi	MC-Glauber PYTHIA	(3+1)-d, η	JAM	Yield, v_n	P+Pb, p/d/He+Au

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Hydrodynamic Model@QM17

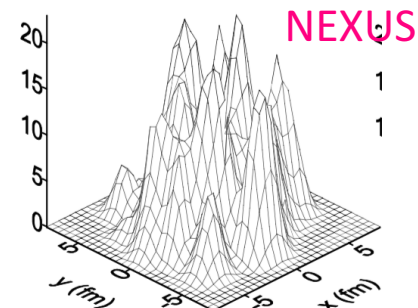
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Hydrodynamic Model@QM17

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Denicol	IP-Glasma
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Kawaguchi	MC-Glauber PYTHIA
Karpenko	UrQMD
Auvinen	UrQMD
Bernhard	TRENTO
Moreland	TRENTO
Wang	AMPT

Fluctuating initial conditions

- Model
 - NLO pQCD + saturation
 - IP-Glasma: gluon, glasma
 - MC-Glauber: nucleon
 - TRENTO: Bayesian 解析に便利。IP-Glasma、KLN、Glauber風の初期条件。Normalization は決まらない。
 - MC-Glauber+PYTHIA for small systems
- Event generator
 - AMPT: HIJING(jet interaction)-ZPC(parton cascade)-ART(hadronic scattering)
 - NEXUS: Regge-Gribov theory
 - UrQMD: ハドロンベース - 低い衝突エネルギー
- New
 - MC-Glauber+Lexus for BES experiment
低エネルギー衝突、流体は少しずつ作られる



TRENTO

T_RENTo: parametric initial condition model

Ansatz: entropy density proportional to **generalized mean** of local nuclear density

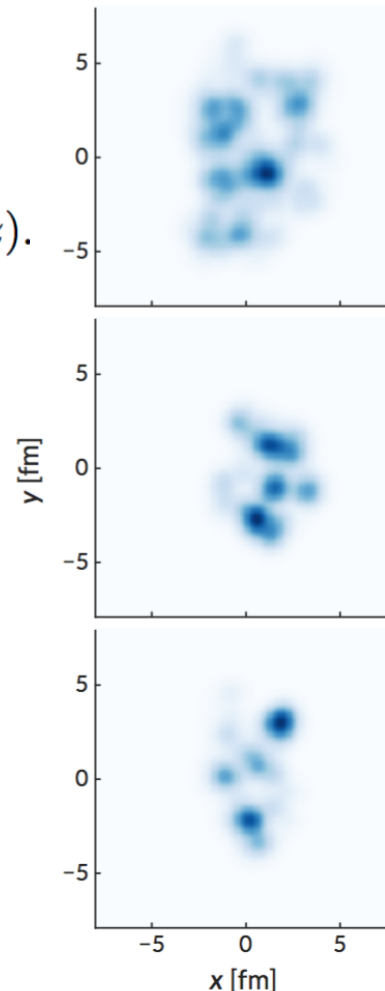
$$s \propto \left(\frac{T_A^p + T_B^p}{2} \right)^{1/p} T_{A,B}(x, y) = \int dz \rho_{A,B}^{\text{part}}(x, y, z).$$

$p \in (-\infty, \infty)$ = tunable parameter;
varying p mimics other models:

- $p = 1 \implies s \propto T_A + T_B$
wounded nucleon model
- $p = 0 \implies s \propto \sqrt{T_A T_B}$
similar to IP-Glasma, EKRT
- Previous work: $p = 0.0 \pm 0.2$

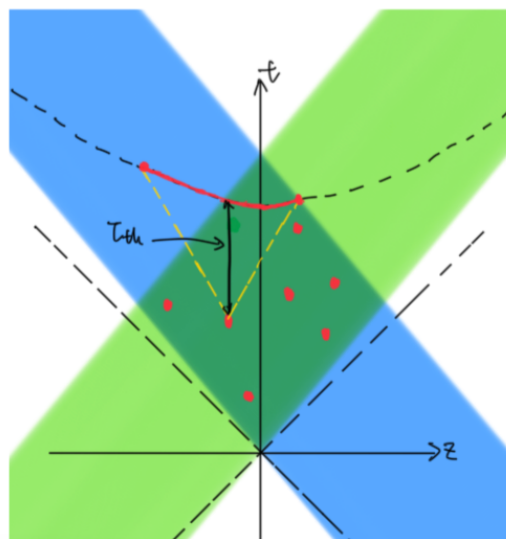
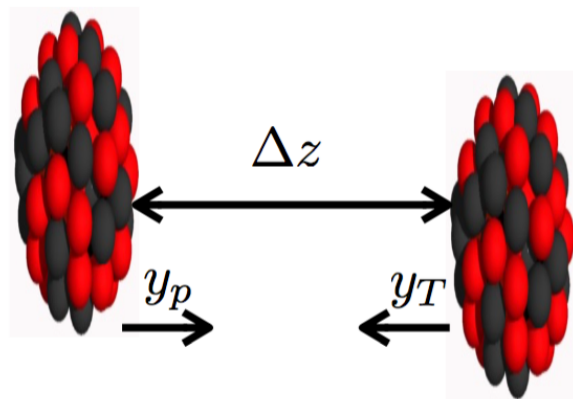
PRC 92 011901 [1412.4708] PRC 94 024907 [1605.03954]

See talk by S. Moreland, Wed. 10:40



MC-Glauber+Lexus

The 3D MCGlauber-LEXUS model



- Collision time and 3D spatial position are determined for every binary collision
- The rapidity loss is determined by the LEXUS model

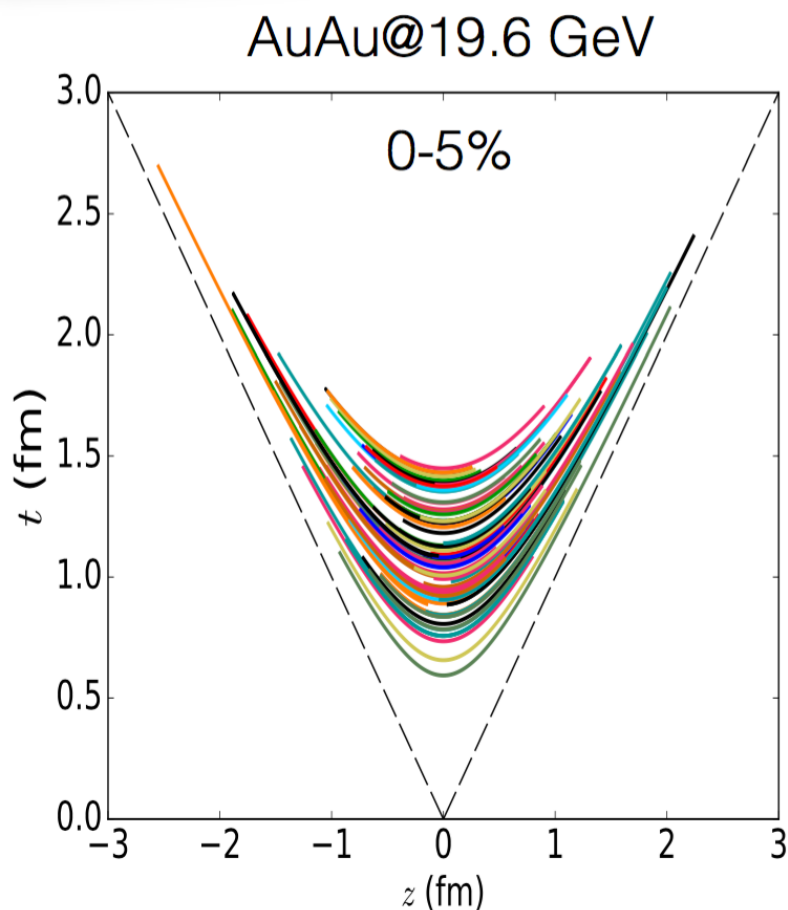
$$P(y_p, y_T, y) = \lambda \frac{\cosh(y - y_T)}{\sinh(y_P - y_T)} + (1 - \lambda) \delta(y - y_P)$$

- QCD strings are free-streaming by $\tau_{th} = 0.5 fm$ before thermalized to medium

低エネルギー衝突での流体の取り扱い
流体: 2つの原子核が通りに抜けた後?

MC-Glauber+Lexus

The 3D MCGlauber-LEXUS model



- Collision time and 3D spatial position are determined for every binary collision
- The rapidity loss is determined by the LEXUS model

$$P(y_p, y_T, y) = \lambda \frac{\cosh(y - y_T)}{\sinh(y_P - y_T)} + (1 - \lambda)\delta(y - y_P)$$

- QCD strings are free-streaming by $\tau_{\text{th}} = 0.5 \text{ fm}$ before thermalized to medium

MC-Glauber+Lexus

Hydrodynamics with sources

Energy-momentum current and net baryon density are feed into hydrodynamic simulation as source terms

$$\partial_\mu T^{\mu\nu} = J_{\text{source}}^\nu$$

$$\partial_\mu J^\mu = \rho_{\text{source}}$$

流体がsource termを通じて徐々に作られる。

where

$$J_{\text{source}}^\nu = \delta e u^\nu + (e + P) \delta u^\nu$$

$$\delta u^\nu = \frac{\Delta_\mu^\nu J_{\text{source}}^\mu}{e + P}$$

heats up the system

accelerates the flow velocity

ρ_{source} dopes baryon charges into the system

- Source terms are smeared with Gaussians in space and time

Hydrodynamic Model@QM17

Speaker	Hydro
Eskola	(2+1)-d, η
Denicol	MUSIC, h, z
McDonald	MUSIC, η, ζ
Shen	MUSIC, η, κ
Gardim	SPHERIO
Luzum	SPHERIO
Sakai	Thermal fluc, η
Kawaguchi	(3+1)-d, η
Karpenko	(3+1)-d, η
Auvinen	(3+1)-d, η
Bernhard	(2+1)-d, η, ζ
Moreland	(2+1)-d, η, ζ
Wang	(3+1)-d, η

EoS from lattice QCD、viscous hydrodynamics

+ transient fluid-dynamics EoM $\pi^{\mu\nu}$, SHASTA

+ transient fluid-dynamics EoM $\pi^{\mu\nu}$, KT scheme

Ideal, Smoothed particle hydrodynamics, 有限個の粒子によって表現

+ thermal fluctuations,

ν HLL, EoS は密度も入っているはず。

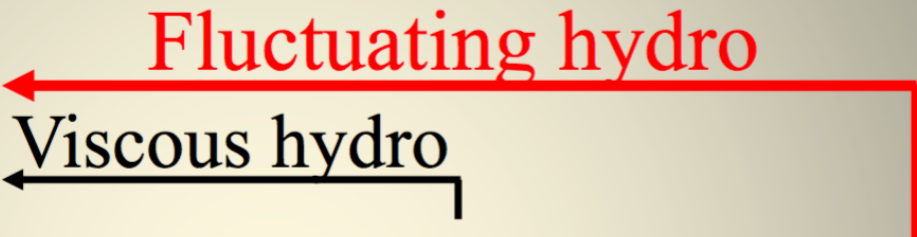
VISHNU(Ohio group), SHASTA

KT scheme

Hydrodynamic Fluctuations

Hydrodynamic fluctuations

Shear stress tensor

$$\pi^{\mu\nu}(x) = \langle 2\eta \partial^{\langle\mu} u^{\nu\rangle} \rangle + \delta\pi^{\mu\nu}(x)$$


η : shear viscosity

Ensemble

Fluctuations

u^μ : four fluid velocity

average

around mean value

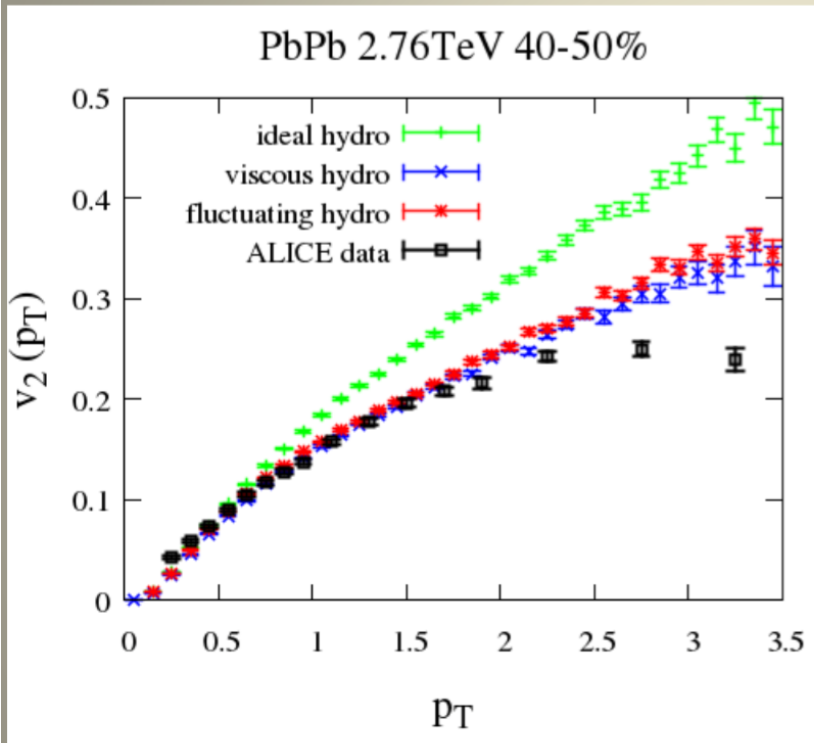
→ Hydrodynamic
fluctuations

Note: Relaxation term needed in actual simulations

Hydrodynamic Fluctuations

Parameters in initial conditions <- Centrality dependence of multiplicity

p_T -differential v_2



Ideal hydro

→ Larger than ALICE data

Viscous & Fluctuating hydro ($\eta/s = 1/4\pi$)

→ Good agreement with ALICE data below $p_T \sim 1.5$ GeV

ALICE Collaboration,
Phys. Rev. Lett. 116 (2016) 132302

by Sakai

流体から粒子へ

Speaker	Particlization
Eskola	CF, decay, vis
Denicol	UrQMD
McDonald	UrQMD
Shen	Hadron cascade
Gardim	MC sampling
Luzum	MC sampling
Sakai	JAM
Kawaguchi	JAM
Karpenko	UrQMD
Auvinen	UrQMD
Bernhard	UrQMD
Moreland	UrQMD
Wang	CF, decay

- Cooper-Frye で粒子分布を計算
 - Freezeout hypersurface の書き出し
 - 共鳴粒子
 - 粘性効果

$$E \frac{d^3 N}{dp^3} = \int_{\sigma} d\sigma_{\mu} p^{\mu} f(x, p)$$

$$f_i(x, p) = f_{0i}(x, p) + \delta f_i$$

$$f_{0i}(x, p) = \frac{g_i}{(2\pi)^3} \left[\exp\left(\frac{p_i^{\mu} u_{\mu} - \mu_i}{T}\right) \pm 1 \right]^{-1}$$

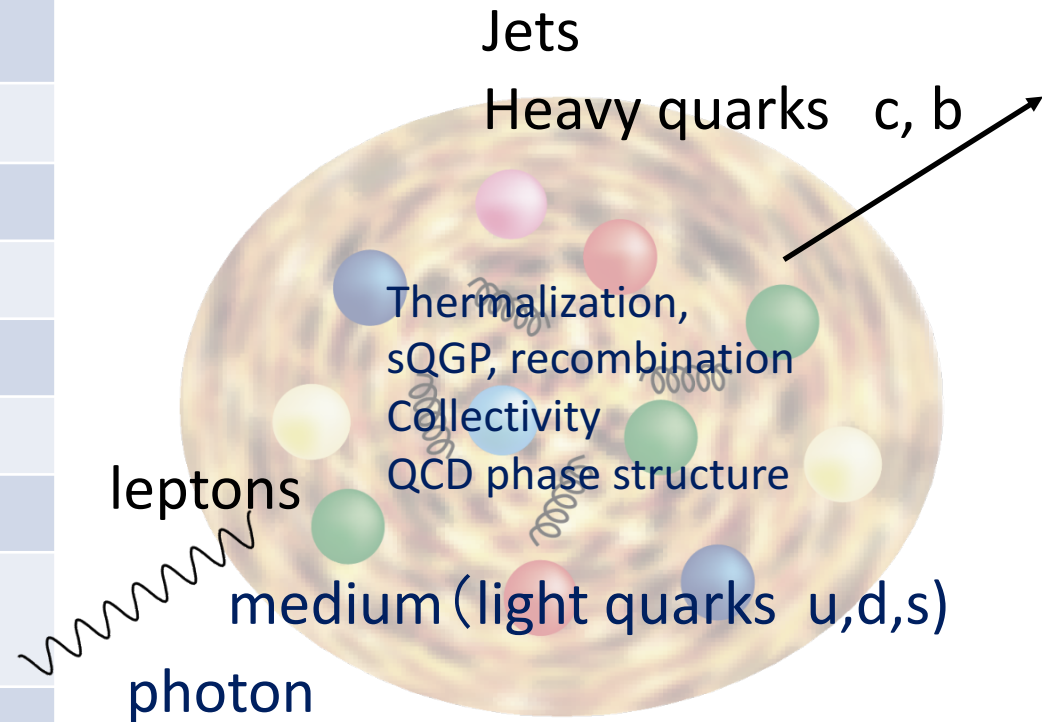
- 崩壊
- MC sampling

- Event generator ^
- JAM
 - UrQMD

Final state interactions

物理量

Speaker	observables	system
Eskola	v_n , correlation	Au+Au, Pb+Pb
Denicol	v_2, v_3	RHIC/LHC
McDonald	Flow 全般	Pb+Pb
Shen	Yield	Au+Au(BES)
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Wang	Λ , vorticity	Au+Au



流体モデルは様々な物理量と密接な関係がある。

物理量

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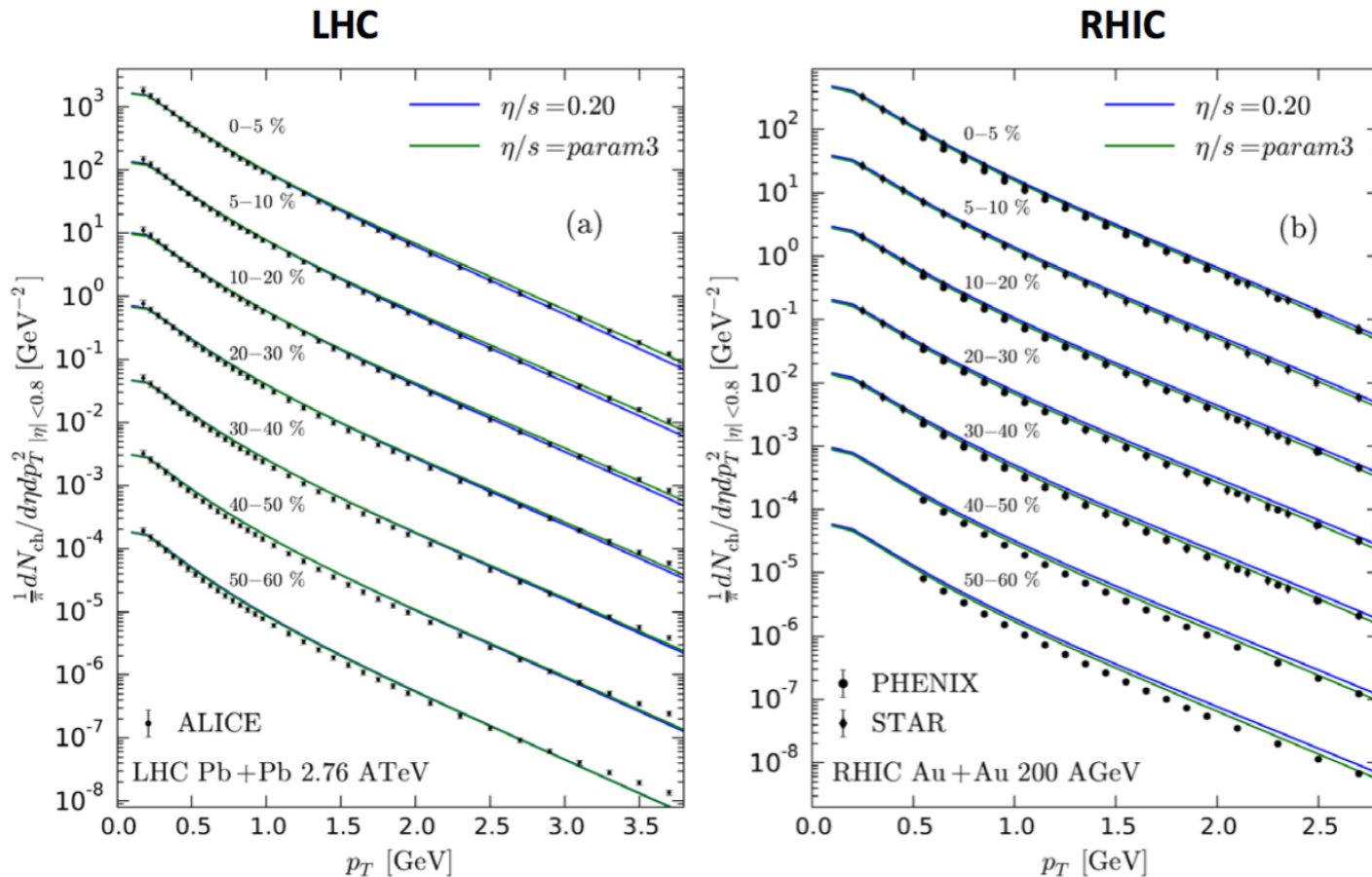
流体にとって基本的（当たり前感）

- One-particle distributions
 π , K, p, strangeness particles...
Flow, v_2 , v_3

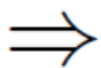
横運動量分布

[Niemi, KJE, Paatelainen, Phys.Rev. C93 (2016) 024907]

Centrality dependence of charged-hadron p_T spectra ~OK



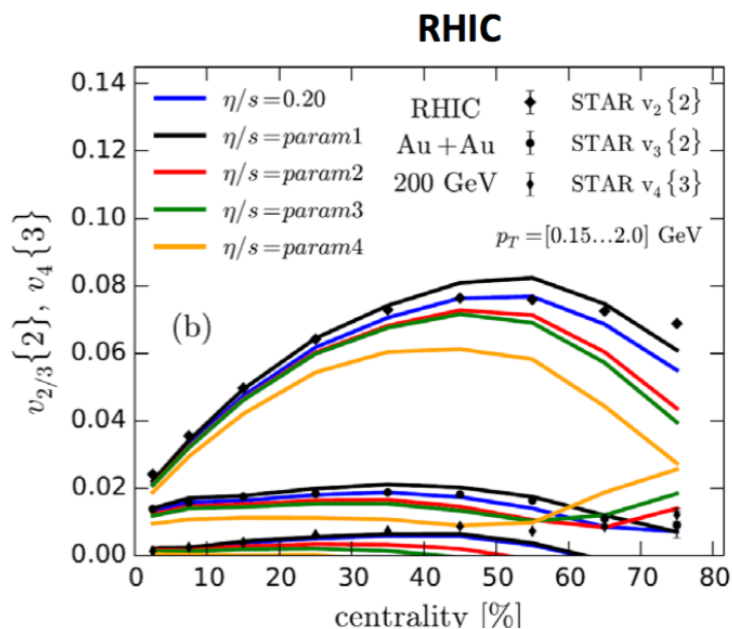
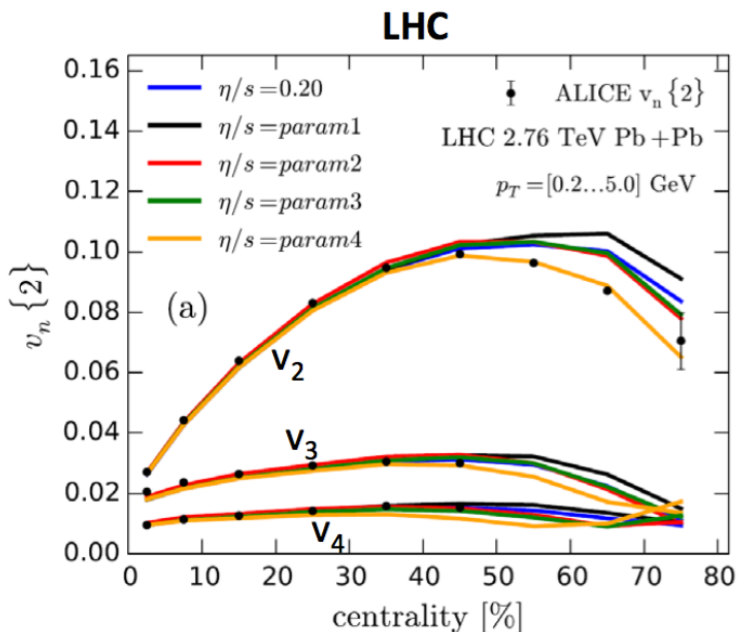
- (2+1)-d
- η/s の振る舞いはパラメタライズ: p_T 分布からではどれが良いのか決められない。



With $T_{\text{chem}} = 175$ MeV we get the low- p_T part ~OK; essentially no constraints for $\eta/s(T)$ from here, either

Flow から η/s の情報

Centrality dependence of 2,3-particle cumulant flow coefficients v_n

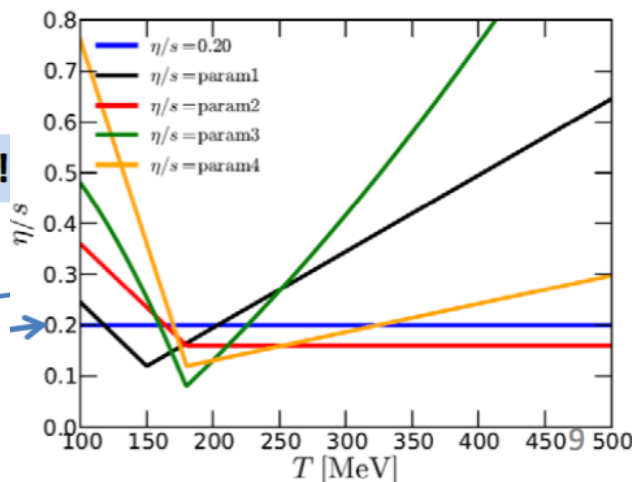


- LHCでは違いがなし。RHICでは違いが。
- Bayesian analysis

LHC v_n s well reproduced by **all** these $\eta/s(T)$

Simultaneous LHC & RHIC analysis very important!

Constraints for $\eta/s(T)$:
 Small $\eta/s(T)$ in the HRG seems favored



by Eskola

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流体にとって基本的（当たり前感）

- One-particle distributions
 π , K, p, strangeness particles...
- Flow, v_2 , v_3

実験を説明するのは少し困難かも？

- Correlations, HBT
- fluctuations

中込さん

Λ , vorticity

- 良い流体アルゴリズムの必要あり
- 衝撃波、小さな人工粘性

Cf. ジェットエネルギー損失

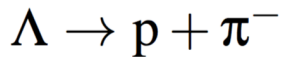
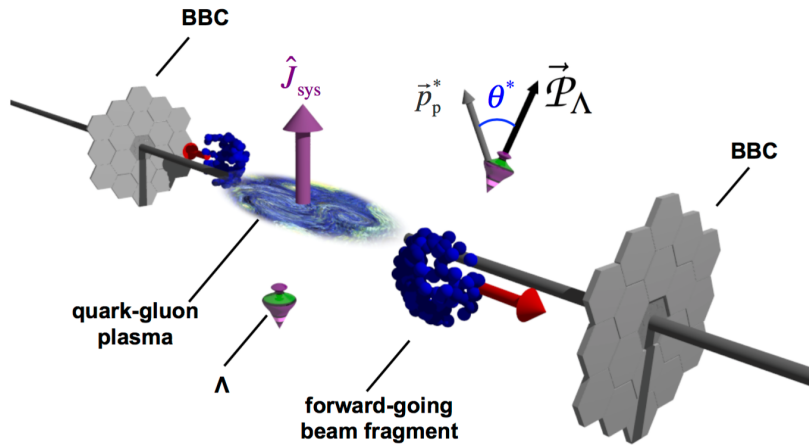
by Tachibana

Global Lambda Polarization

STAR, arXiv:1701.06657

Vortical structure of the QGP fluid

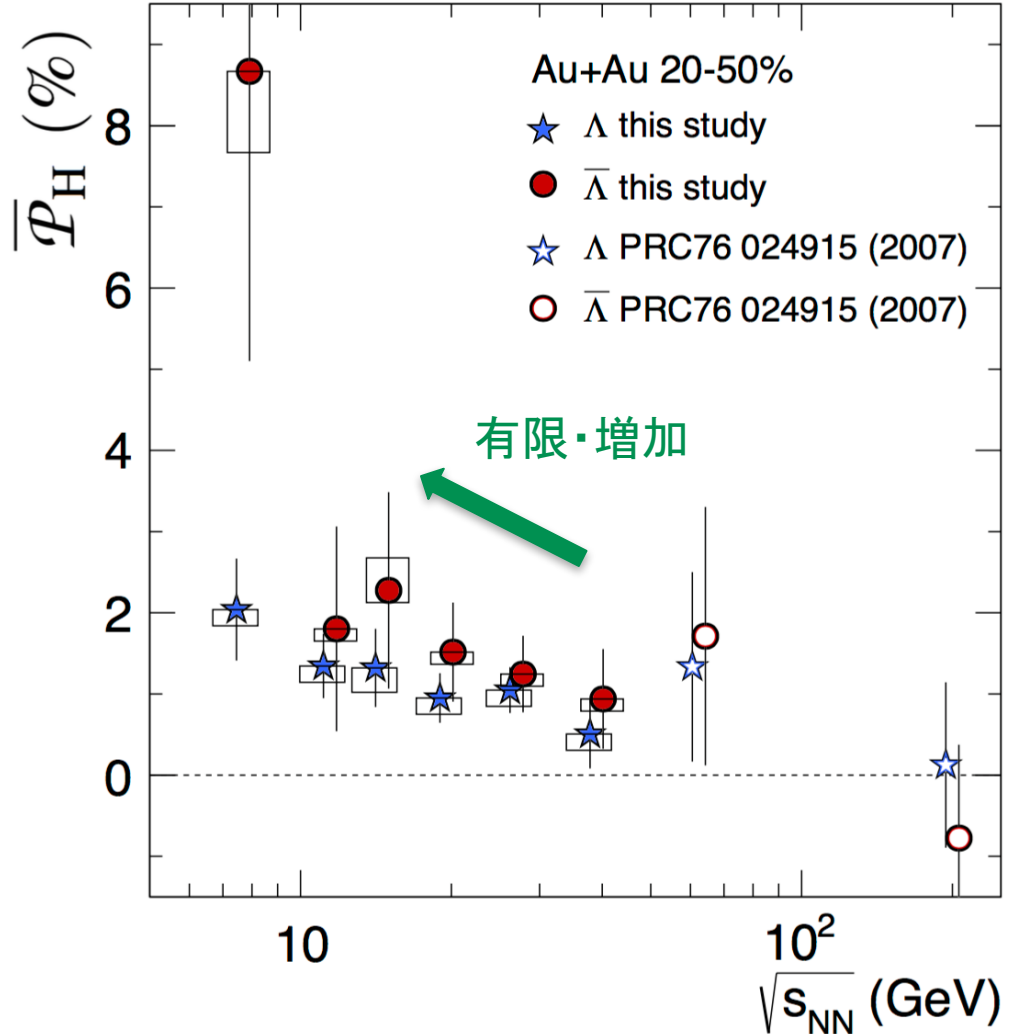
Internal quantum structure of particle



\vec{P}_Λ は運動量に依存しない
平均を取ると \vec{j}_{sys} と平行

$$\bar{P}_H \equiv \langle \vec{P}_H \cdot \hat{j}_{\text{sys}} \rangle = \frac{8}{\pi \alpha_H} \frac{\langle \cos(\phi_p^* - \phi_{j_{\text{sys}}}) \rangle}{R_{\text{EP}}^{(1)}}$$

“Global polarization”



Vorticity Structure in QGP

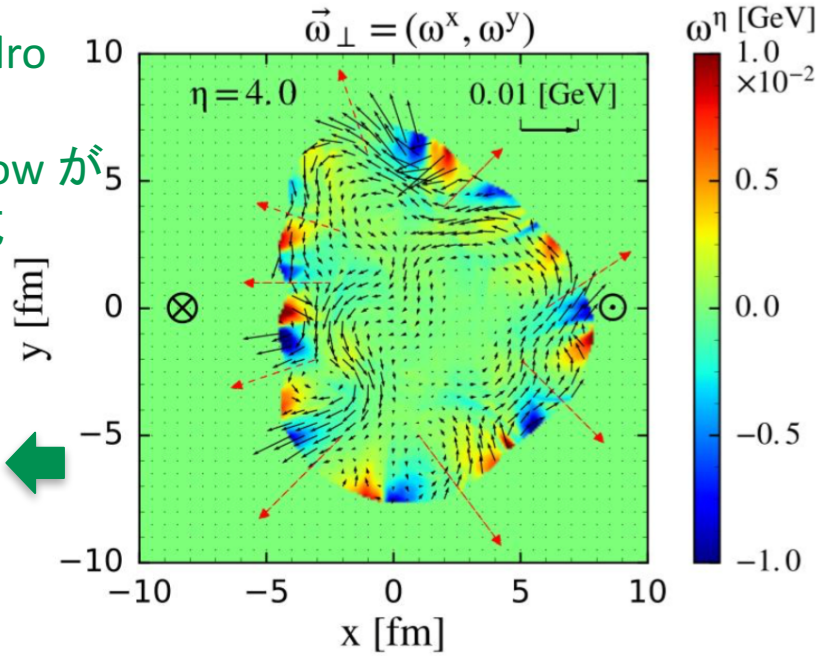
Complex local vorticity structure

AMPT-HIJING
+3D viscous hydro
Au+Au 20-30%
初期のShear flow が
Vorticity を形成

Polarization
of
hypersurface



Λ Polarization

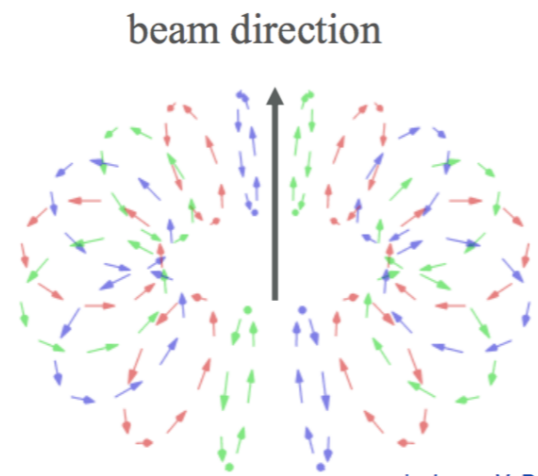


L.G.Pang, H.Petersen, Q.Wang & XNW
PRL 117, 192301 (2016)

- Vortex pair in 2D
- Vortex ring in 3D =
Toroidal (smoke ring)
vortical fluid



- Vortex ring appears in the longitudinal direction
- Ridge-like vortex pairs in the transverse plane.

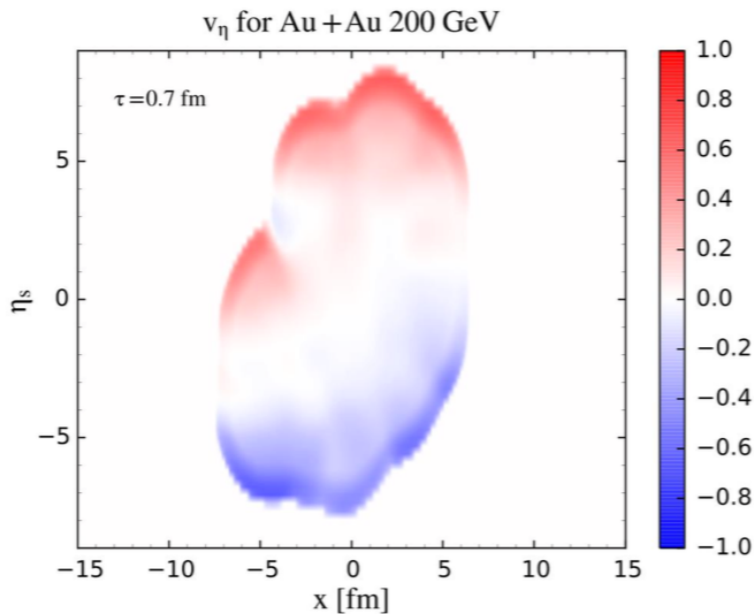
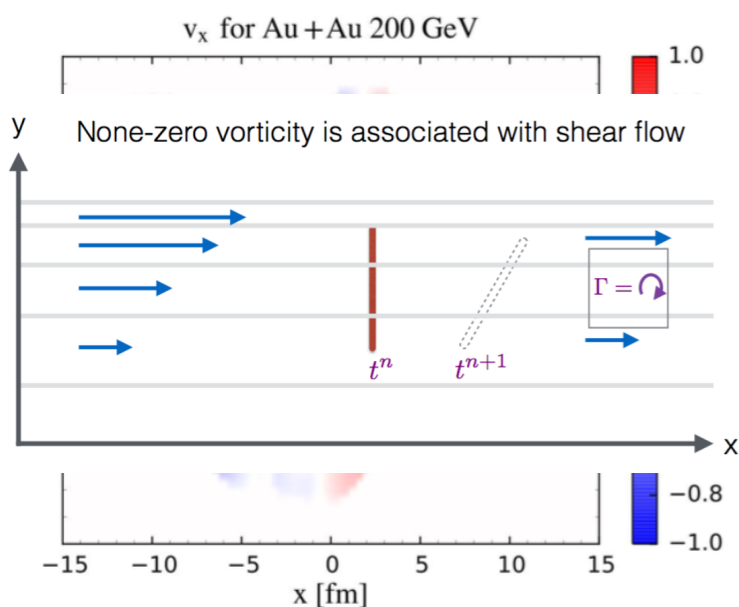


by Lucas V. Barbosa
from Wiki Pedia



Shear Flow to Vorticity

Fluid shear and forward-backward asymmetry



- AMPT initial condition + hydrodynamics
- Start with: $v_x = v_y = v_\eta = 0$ at $\tau = 0.4$ fm

Vorticity Structure in QGP

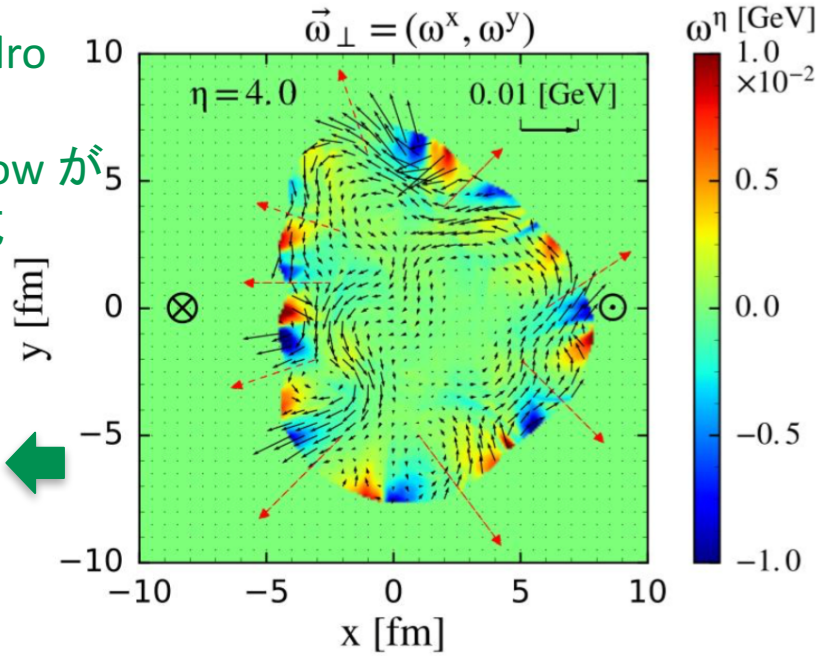
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Polarization
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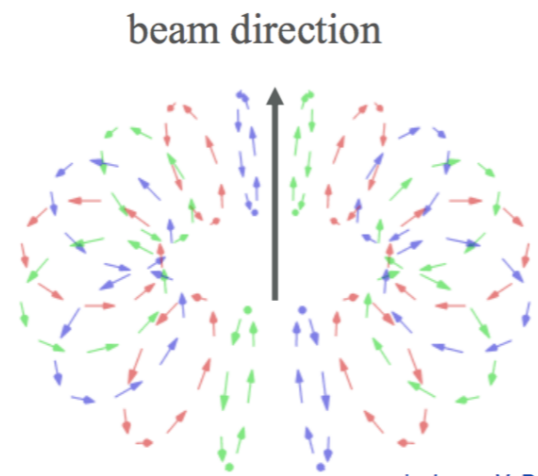


Λ Polarization



L.G.Pang, H.Petersen, Q.Wang & XNW
PRL 117, 192301 (2016)

- Vortex pair in 2D
- Vortex ring in 3D =
Toroidal (smoke ring)
vortical fluid



by Lucas V. Barbosa
from Wiki Pedia

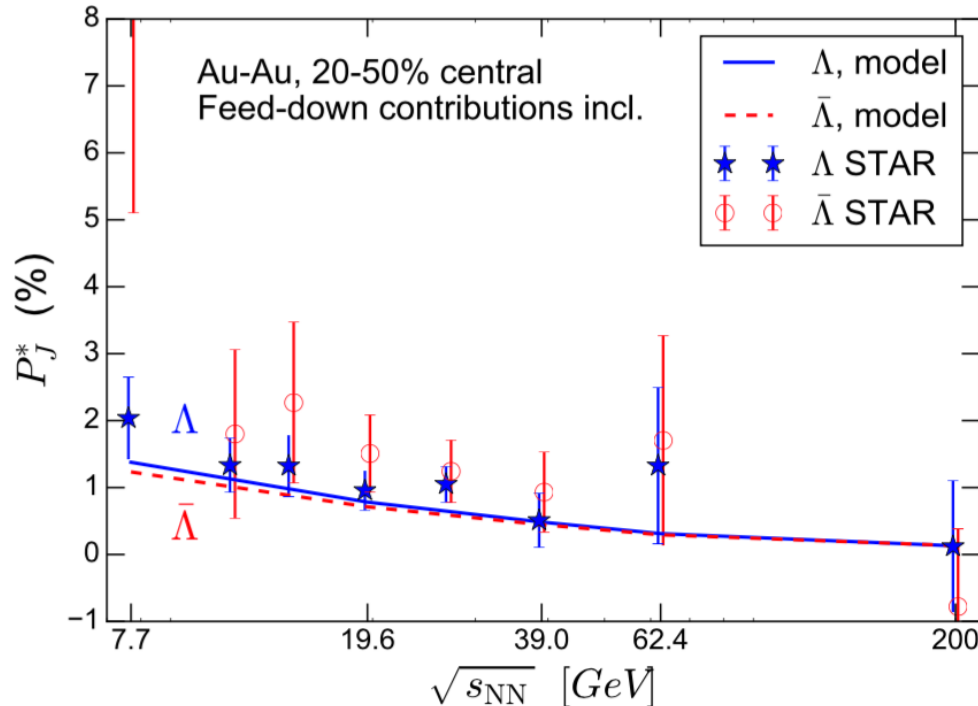
- Vortex ring appears in the longitudinal direction
- Ridge-like vortex pairs in the transverse plane.



実験との比較

Λ and $\bar{\Lambda}$: UrQMD+vHLLLE vs experiment

NEW



実験結果をおおよそ再現

- Λ within experimentan error bars.
- Much smaller and opposite sign $\bar{\Lambda}$ - Λ splitting. Only μ_B effect in the model, and it is small.
- MHD interpretation: vorticity creates the average $\Lambda + \bar{\Lambda}$, magnetic field makes the splitting.
- **Magnetic field at particlization?**

Hydrodynamic Model@QM17

Speaker	IC	Hydro	Particization	observables	system
Eskola	NLO pQCD + saturation	(2+1)-d, η	CF, decay, vis	v_n , correlation	Au+Au, Pb+Pb
Denicol	IP-Glasma	MUSIC, η, ζ	UrQMD	v_2, v_3	RHIC/LHC
Bernhard	TRENTO	(2+1)-d, η, ζ	UrQMD	Yield, $\langle P_T \rangle, v_n$	Pb+Pb
McDonald	IP-Glasma	MUSIC, η, ζ	UrQMD	Flow 全般	Pb+Pb
Gardim	NEXUS	SPHERIO	MC sampling	correlation	Au+Au
Luzum	NEXUS	SPHERIO	MC sampling	fluctuations	Au+Au
Sakai	MC-Glauber	Thermal fluc, η	JAM	factorization	Pb+Pb
Wang	AMPT	(3+1)-d, η	CF, decay	Λ , vorticity	Au+Au
Karpenko	UrQMD	(3+1)-d, η	UrQMD	Λ , vorticity	Au+Au(BES)
Auvinen	UrQMD	(3+1)-d, η	UrQMD	Yield, HBT, v_2	Au+Au(BES)
Shen	MC-Glauber+Lexus	MUSIC, η, κ	Hadron cascade	Yield	Au+Au(BES)
Moreland	TRENTO	(2+1)-d, η, ζ	UrQMD	Yield, v_n	P+Pb
Kawaguchi	MC-Glauber PYTHIA	(3+1)-d, η	JAM	Yield, v_n	P+Pb, p/d/He+Au

Bayesian Analysis

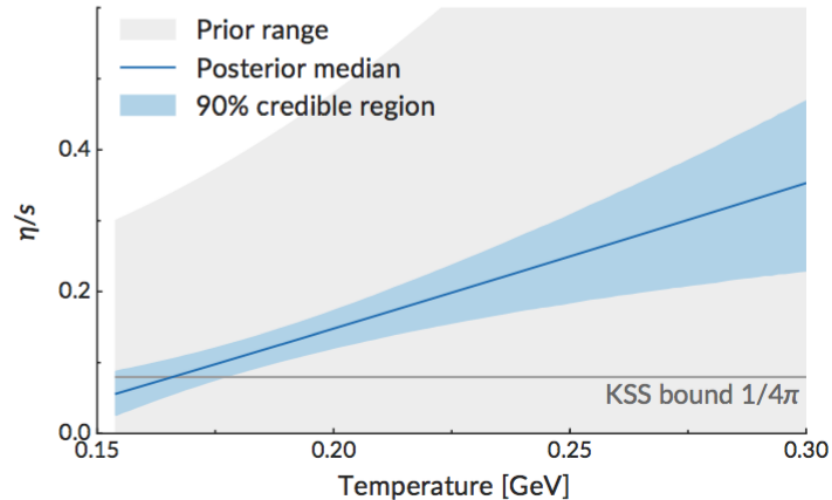
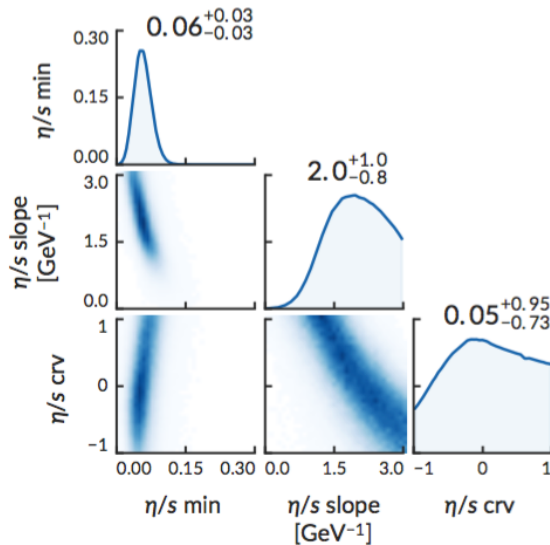
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Shear Viscosity

LHC Pb+Pb 2.76 and 5.02 GeV

Shear viscosity

$$(\eta/s)(T) = (\eta/s)_{\min} + (\eta/s)_{\text{slope}}(T - T_c) \times \left(\frac{T}{T_c}\right)^{(\eta/s)_{\text{crv}}}$$



- Zero η/s excluded; min consistent with AdS/CFT
- Constant η/s excluded
- Best constrained $T \lesssim 0.23$ GeV
- RHIC data could disambiguate slope and curvature

by Bernhard

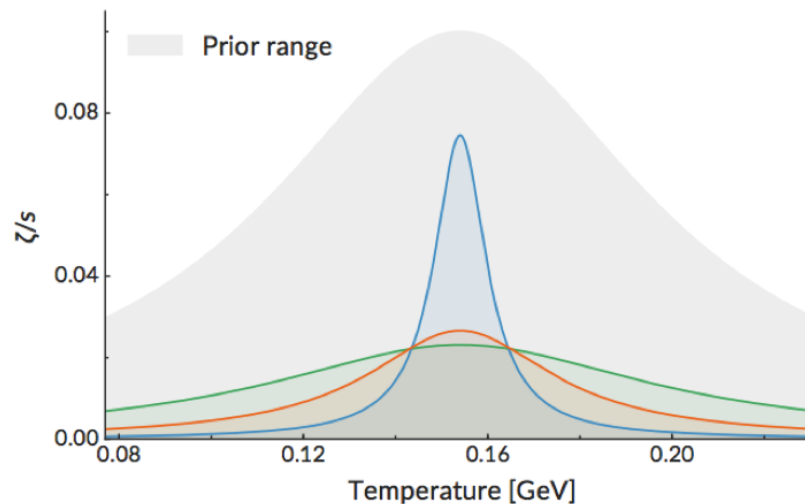
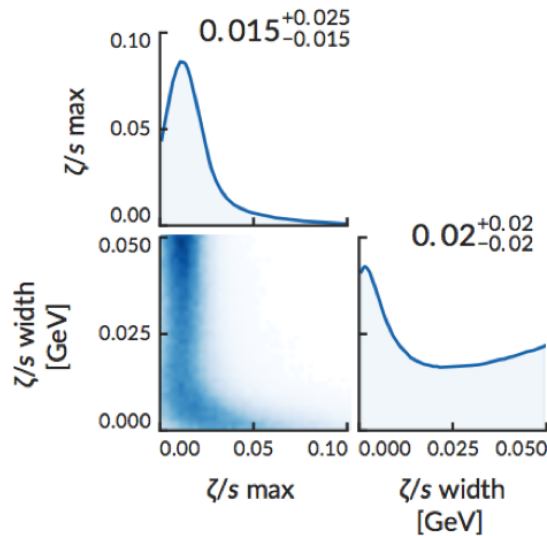
Bulk Viscosity

LHC Pb+Pb 2.76 and 5.02 GeV

Bulk viscosity

$$(\zeta/s)(T) = \frac{(\zeta/s)_{\max}}{1 + \left(\frac{T - T_c}{(\zeta/s)_{\text{width}}}\right)^2}$$

ピークの位置は固定



- Can be “tall” or “wide”, but not both
- Short and wide (green) slightly favored

See also talk by G. Denicol, Wed. 17:30

Bayesian characterization of the initial state and QGP medium

18/2 by Bernhard

Bayesian Analysis

Speaker	IC	Hydro	Particization	observables	system
Denicol	IP-Glasma	MUSIC, η,ζ	UrQMD	v_2,v_3	RHIC/LHC
Bernhard	TRENTO	(2+1)-d, η,ζ	UrQMD	Yield, $\langle P_T \rangle, v_n$	Pb+Pb
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- Bernhard:もっとも綺麗な結果を得るのに成功している。
 $\eta/s, \zeta/s$ の温度依存性

Bulk Viscosity

Model

Ryu *et al*, PRL 115, no. 13, 132301 (2015)

IP-Glasma + MUSIC + Cooper-Frye

$\tau_0 = 0.4 \text{ fm}$

$T_{fo} = 145 \text{ MeV}$

← 固定

Emulator from MADAI

See S. Pratt lecture, S. Bass plenary talk
Novak *et al*, PRC89, 034917 (2014), 1303.5769.

500 random parameter samples (100 events per parameter sample)

Observables considered (20-30%)

← 1つのcentrality

RHIC

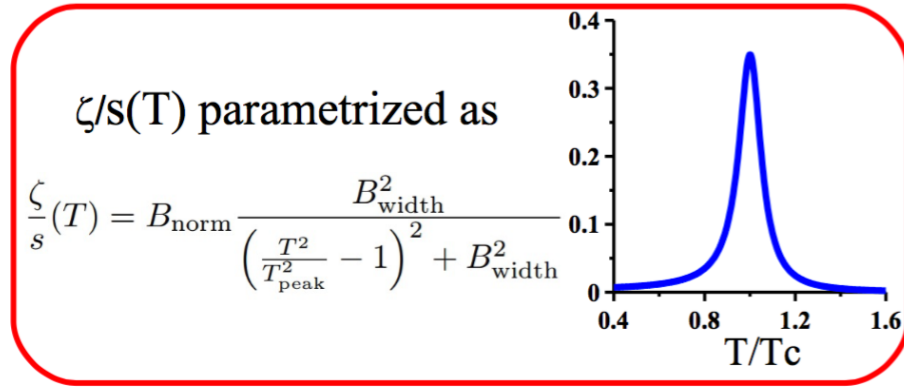
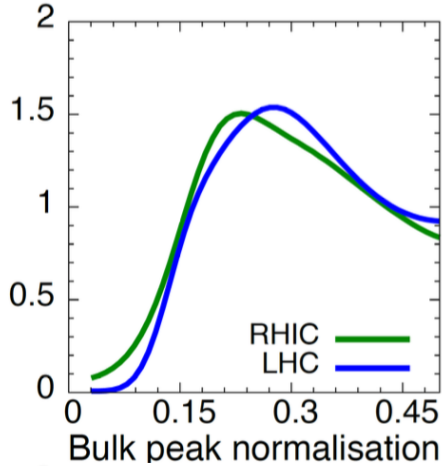
LHC

Observable	N^{π^+}	$\langle p_T^{\pi^+} \rangle$	$v_2\{2\}$	$v_3\{2\}$
$p_T \text{ cut (GeV)}$	$p_T > 0$	$p_T > 0$	$p_T > 0.15$	$p_T > 0.15$
Value	135	0.411 GeV	0.0642	0.0183
Uncertainty	10	0.021 GeV	0.000075	0.0001

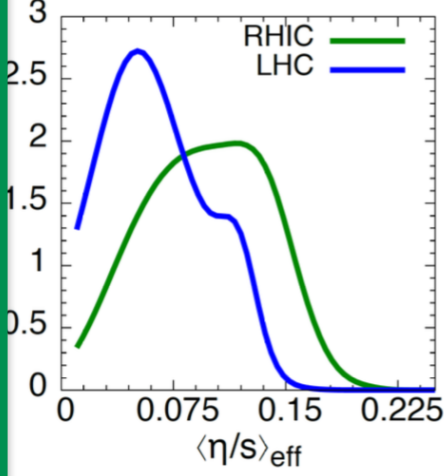
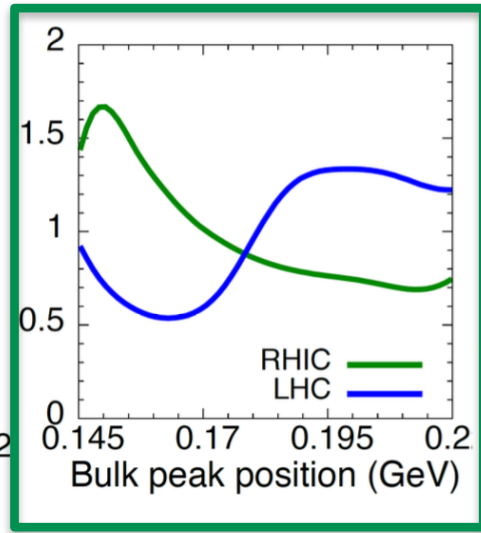
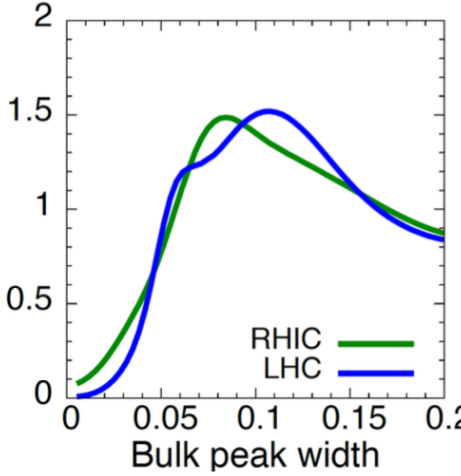
Observable	N^{π^+}	$\langle p_T^{\pi^+} \rangle$	$v_2\{2\}$	$v_3\{2\}$
$p_T \text{ cut (GeV)}$	$p_T > 0$	$p_T > 0$	$p_T > 0.2$	$p_T > 0.2$
Value	307	0.512 GeV	0.0831	0.0293
Uncertainty	20	0.017 GeV	0.0034	0.0015

Bulk Viscosity

Results – probability distributions



ピークの位置もパラメータ



RHICとLHCで ζ/s のピークの位置が異なる？！

by Denicol



Bayesian Analysis

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- Bernhard:もっとも綺麗な結果を得るのに成功している。
 $\eta/s, \zeta/s$ の温度依存性
- Denicol: ζ/s の振る舞いがRHICとLHCで異なる? Bayesian analyses の正しい評価?
Bernhard との違い: Initial condition を固定している。
一つのcentralityのみ
おそらくは(3+1)次元の流体計算が重いためでは?

Bayesian Analysis

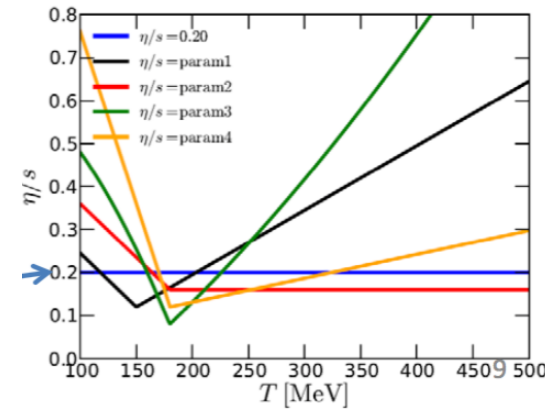
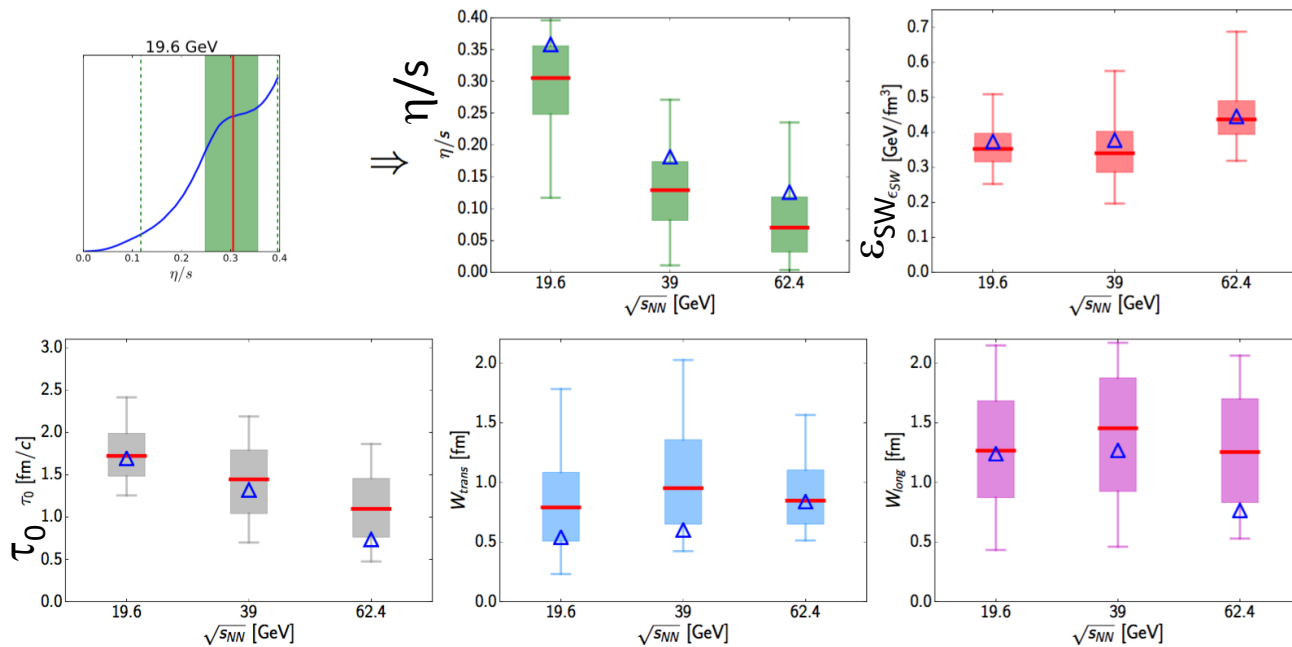
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- Auvinen: BES 実験に適用。

BES

Parameter dependence on collision energy

η/s and τ_0 show clear increasing trend towards lower energies (however, minimum of τ_0 increases by construction)



by Eskola

η/s : 低衝突エネルギーほど増加

Boxes: 50% confidence range

Whiskers: 95% confidence range

by Auvinen



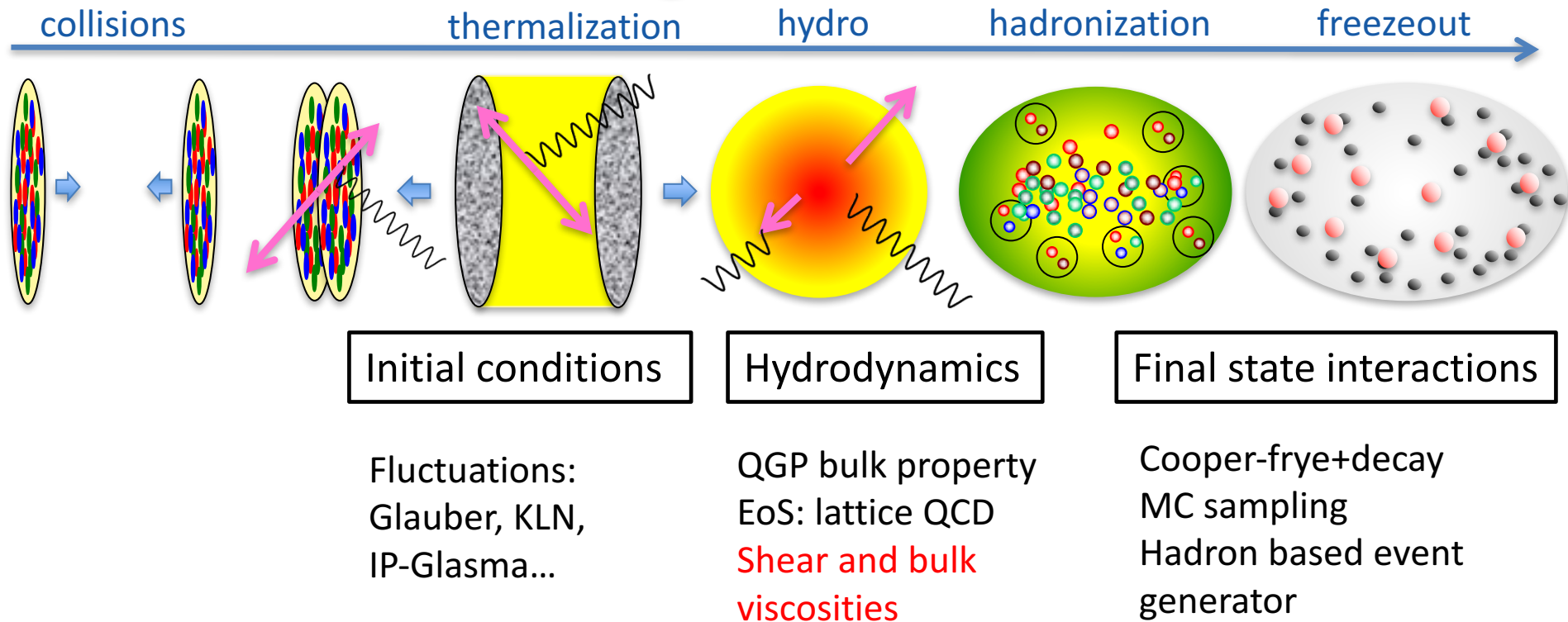
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Bernhard との違い: Initial condition を固定している。
一つの centrality のみ
おそらくは (3+1) 次元の流体計算が重いためでは?
- Auvinen: BES 実験に適用。
 $\eta/s \sim 0$ <- Bernhard と η/s の振る舞いが inconsistent
- Moreland: small system に適用。挑戦的な計算。まだ途中か

強力な解析手法だが、モデル、input が大事。信頼の置ける結果を得るには多くの実験結果、膨大な計算量が必要。

まとめ



- 流体模型の発展は著しい
- 現実的な実験解析が可能に
 - Bayesian 解析: 実験結果からモデルのパラメータ、QGPの物性を探る。
- 流体模型の枠組みの発展
 - 流体ゆらぎ
 - Anisotropic hydrodynamics